

# Cyber Risks in the Smart Home Ecosystem: Identification, Modeling, and Pricing

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# Cyber Risks in the Smart Home Ecosystem: Identification, Modeling, and Pricing

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# Cyber Risks in the Smart Home Ecosystem: Identification, Modeling, and Pricing

## Executive Summary

The fourth industrial revolution has emerged (a.k.a., Industry 4.0) in the last few decades and one particular area that it encompasses is the Internet of Things (IoT) and smart manufacturing. The omnipresence of IoT technologies encourages homeowners to transform their homes into smart homes to provide more convenient, comfortable, and secure environments. The global smart home market has exhibited progressive growth in the past few years and has attracted more and more attention from commercial parties. This leads to the emergence of the smart home ecosystem, which consists of various smart devices such as computers, locks, sensors, thermostats, wearables, and various home appliances.

However, many studies in the technological cybersecurity domain have shown that IoT technologies come with their own vulnerabilities, which can be exploited by attackers to compromise smart home devices (e.g., to open garage doors for attackers) and cause damage to homeowners. This new dimension of threats brings an important opportunity for insurance companies to grow their cyber insurance businesses while helping mitigate the risks that are imposed on homeowners by these vulnerabilities.

From an insurer's perspective, state-of-the-art approaches are needed since cyber risks in the smart home ecosystem are little investigated and understood. The present project aims to fill this void. Specifically, we develop a novel and practical quantitative framework for modeling the cyber risks associated with the smart home ecosystem, with an emphasis on cyber insurance pricing. The framework consists of four components: (i) identifying vulnerability-incurred cyber risks; (ii) classifying cyber risks into business lines; (iii) modeling cyber risks; and (iv) determining insurance premiums and coverages. This project lays a sound practical groundwork for launching cyber insurance for the smart home ecosystem, which will provoke further in-depth investigation along this research line.

This project enhances the current understanding of cyber risks in the smart home ecosystem from the insurance industry's perspective. In particular, the quantitative framework and pricing strategies developed in this project can be immediately adopted/adapted by actuaries to price the cyber risks for smart homes, a fast-growing insurance market.



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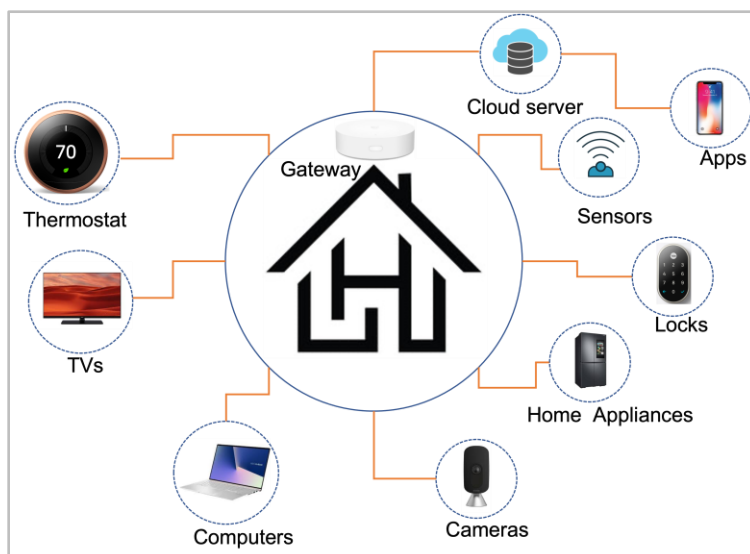
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## Section 1: Introduction

The omnipresence of IoT technology allows average households to transform into smart homes to provide more convenient, comfortable, and secure living environments. According to a report by Zion Market Research, the global smart home market is likely to reach US\$137.9 billion by 2026, with a compound growth of slightly more than 1.4% from 2020 to 2026<sup>1</sup>. This explains why the smart home ecosystem is attracting more and more attention from commercial parties such as energy suppliers, third-party software and hardware vendors, and insurance companies.

**Figure 1**

**ILLUSTRATION OF THE COMPLEXITY AND HETEROGENEITY OF THE SMART HOME ECOSYSTEM.**



One feature of the smart home ecosystem is that the devices connected to smart homes are highly heterogeneous in their services, ranging from security, healthcare, convenience, and entertainment, to energy efficiency [1]. As illustrated in Figure 1, there are a variety of smart devices in the smart home ecosystem, including thermostats, TVs, computers, cameras, locks, sensors, and smart home appliances. These devices collect and exchange data with each other, allowing homeowners to use smart devices to seamlessly “merge” the physical world and the digital world associated with smart homes into a unified environment. In this ecosystem, the cloud server provides the platform that allows a user to interact with the smart devices at home via mobile applications; each smart device runs independently and communicates via a local mesh network (e.g., Zigbee) with a home gateway acting as the central node. Together, these illustrate the high complexity and heterogeneity of smart devices in smart home ecosystems.

While the smart home ecosystem offers convenience and comfort to our daily lives, smart devices, like many other new technologies, come with many vulnerabilities that can be exploited by attackers to cause damage to homeowners, which leads to an unreliable and insecure ecosystem [2, 3]. For instance, an attacker can wage Denial-of-Service (DoS) attacks to disrupt the use of smart devices; an attacker can wage eavesdropping attacks (e.g., Man-in-the-Middle attack) to steal personal information or corrupt data; an attacker can exploit vulnerabilities in smart cameras for cyber extortions [4]. Indeed, the Avast Smart Home Security Report 2019, which is based on an extensive smart home market analysis, shows that 4.8% of

<sup>1</sup> <https://www.zionmarketresearch.com/report/smart-home-market>

smart homes have at least one device that is vulnerable to cyber attacks<sup>2</sup>. Notably, among these vulnerabilities, 69.2% are vulnerable because of weak credentials and 31.4% because of software vulnerabilities.

The vulnerabilities such as those mentioned above lead to cyber risks, which represent opportunities for insurance companies to expand their insurance services to help smart homeowners in transferring their cyber risks. The status quo is that the current smart home insurance market mainly provides limited coverage for smart homeowners, which are typically treated as add-ons to standard home insurance policies. For instance, one major insurance company offers smart home coverage, including data breaches, computer and home systems attacks, cyber extortion, and online fraud, but the coverage limits top out at \$50,000 with a \$500 deductible; another major insurance company offers a personal cyber insurance add-on to its standard home insurance policy by covering some cyber risks in the smart home ecosystem, including cyber-attacks and extortion, with limits up to \$15,000. These examples show that the current smart home insurance market is still in the infancy stage, demanding effort and help from the actuarial community.

The insurance coverage demand mentioned above has led to many studies assessing the risks associated with the smart home ecosystem. However, most if not all of these studies are from the perspectives of security, privacy, and users [1, 2, 3, 5, 6]. By contrast, the only study found on quantifying cyber risks in the smart home ecosystem from the insurance perspective is from Zhang et al, which studies cyber risks in a general IoT framework and discusses the associated cyber risks in a small home from a theoretical perspective [7].

This work aims to develop *a practical quantitative framework for identifying, modeling, and pricing cyber risks in a smart home ecosystem*. The present study is unique because of the following characteristics:

- It considers *insurers' perspective*. Cyber risks in the smart home ecosystem are studied from an insurer's perspective, which prompts us to first identify vulnerability-incurred cyber risks in a smart home and then discuss the potential impacts of these cyber risks. The impacts allow us to classify the cyber risks into different lines of insurance risks.
- It makes innovative *technical contributions*. We develop practical probabilistic approaches to pricing cyber risks in the smart home ecosystem. We conduct the following two types of analysis: (i) Conservative analysis, which assumes that any vulnerability in the smart home ecosystem will be exploited by the attackers during a policy period. This analysis is simple but practical but corresponds to the worst-case scenario (i.e., the upper bound for the probabilities that the vulnerabilities will be exploited, respectively). (ii) Bayesian Attack Graph (BAG) analysis [8], which leverages graphical models that represent the information about vulnerabilities and the interactions between the devices in the smart home ecosystem (i.e., the attack paths that can be leveraged to compromise the devices in the smart home ecosystem). Note that (ii) is finer grained than (i) but requires a strong security assessment team.
- It is ready for *real-world adoption*. The present study is more practical and can be easily adopted/adapted by insurance companies to accommodate any relevant scenarios. This is evidenced by our exploration of pricing strategies.

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<sup>2</sup> [https://cdn2.hubspot.net/hubfs/486579/avast\\_smart\\_home\\_report\\_feb\\_2019.pdf](https://cdn2.hubspot.net/hubfs/486579/avast_smart_home_report_feb_2019.pdf)

## Section 2: A quantitative framework for studying the cyber risks in the smart home ecosystem

For the smart home ecosystem, there are extensive studies in the literature on identifying cyber risks from different perspectives, including risk analysis [8, 9], security [2, 10], privacy [5], industry [6], and scenario-based analysis [3]. However, there is only one prior study on modeling cyber risks in a smart home ecosystem from an insurer's perspective and it provides limited discussion. The present study seeks to fill the void on research from an insurer's perspective. In this study, we discuss a quantitative framework for modeling and pricing cyber risks in a smart home ecosystem. This framework consists of four components: 1) Identifying vulnerability-incurred cyber risks; 2) Classifying cyber risks into business lines; 3) Modeling cyber risks; 4) Determining premiums and coverages.

### 2.1 IDENTIFYING VULNERABILITY-INCURRED CYBER RISKS

Because of the inherent complexity and heterogeneous structure, the smart home ecosystem has a large attack surface [9, 11]. From an insurer's perspective, it is of utmost importance to identify the risks via a simple but efficient approach. For this purpose, we propose identifying the risk based on vulnerabilities in the smart home network.

A common approach to assessing vulnerability is based primarily on the Common Vulnerability Scoring Systems (CVSS) [12]. The CVSS computes the severity of a vulnerability as a function of its characteristics, and the confidentiality, integrity, and availability impact on an information system. The base score of CVSS is the most commonly used component which produces a score ranging from 0 to 10, where higher scores represent high threat levels. Almost all known vulnerabilities are published on the National Vulnerability Database<sup>3</sup>. The vulnerability information is identified via the Common Vulnerabilities and Exposures (CVE), and each CVE includes the CVE identifier, description, and references discussing the vulnerability. However, it should be noted that the CVSS score does not reflect the probability that a vulnerability will be used to attack a network since only a very small proportion of vulnerabilities are exploited in practice<sup>4</sup>. It is necessary to convert the CVSS into the exploitation probability. Jacobs et al. [13] propose a data-driven framework for assessing the probability that a vulnerability will be exploited within a certain time period after public disclosure. This system is named the Exploit Prediction Scoring System (EPSS)<sup>5</sup>. They show that this system is easy to implement and provides satisfactory estimates of exploitation.

The following steps can be performed to identify the cyber risks in a smart home ecosystem.

1. Scan vulnerabilities. Typically, the vulnerability report generated by vulnerability scanners includes vulnerability dependency details and CVSS scores [14].
2. Create the vulnerability graph. The vulnerability graph abstracts the exploitation relationship among vulnerabilities which can be used for the attack analysis [8]. Based on the vulnerability details, the vulnerability graph can be created.
3. Determine exploitation probabilities. The exploitation probabilities of vulnerabilities can be determined from the vulnerability graph based on vulnerability details and the EPSS.

For illustration, assume that there are three vulnerabilities discovered in a smart home: CVE2021-21736, CVE-2018-3919, and CVE-2022-22667. The vulnerability graph can be created based on the attack scenario: the attacker exploits a vulnerability in a smartphone Operating System ( $V_1$ : CVE-2022-22667) over the

<sup>3</sup> <https://nvd.nist.gov/vuln-metrics/cvss>

<sup>4</sup> <https://www.kennasecurity.com/resources/prioritization-to-prediction-report/>

<sup>5</sup> <https://www.first.org/epss/model>

wireless network and compromises the smartphone. This grants the attacker access to the smartphone Operating System, which allows the attacker to pivot into the smart home network to compromise the smart home hub by exploiting the vulnerability ( $V_3$ : CVE-2018-3919). Further, the attacker exploits the vulnerability ( $V_5$ : CVE-2021-21736) in the smart camera to gain control over it. The vulnerability graph can be represented via a path of two edges, namely

$$V_1 \rightarrow V_3 \rightarrow V_5.$$

The CVSS base scores for those vulnerabilities are 7.8 ( $V_1$ ), 9.9 ( $V_3$ ), and 7.2 ( $V_5$ ). The EPSS probabilities are .02, .3, and .05, respectively.

## 2.2 CLASSIFYING CYBER RISKS INTO BUSINESS LINES

From the insurer's perspective, the goal is to price the potential loss. It is possible that some vulnerabilities with high CVSS scores and EPSS probabilities only lead to negligible loss. Therefore, it is essential to understand the impacts of cyber-attacks and classify those risks into business lines. Based on the characteristics of the smart home ecosystem, we have identified the following risk categories:

- *Data breach* ( $L_1$ ). The data breach risk refers to the exposure of personal private user data that can be collected from the smart home ecosystem. The private data includes daily activities, emotions, health conditions, voices, and videos. Data breaches can be caused by the exploitation of vulnerabilities in smart devices or by malware attacks. Data breach coverage pays for the attorney costs, IT professionals, and mitigation of damage caused by the private information leak.
- *Loss of use* ( $L_2$ ). The loss-of-use risk refers to the data recovery, home applicants repair, and system restoration costs due to cyber attacks such as malware and Denial-of-Service (DoS) attacks. Coverage for this risk pays for those costs and removing a virus or reprogramming of desktops, laptops, smartphones, tablets, Wi-Fi routers, and other internet access points, such as smart home devices and security systems.
- *Ransomware* ( $L_3$ ). Ransomware refers to that online criminal "lock" (via cryptographic techniques) smart devices such as computers/laptops/tablets, security systems, and/or thermostats to demand ransom. Ransomware coverage pays for the ransom upon the approval of the insurance company or professional assistance to resolve the ransomware event.
- *Cyber extortion* ( $L_4$ ). Cyber extortion occurs when online criminals threaten to release sensitive personal data, activities, conversations, or videos for financial gain. Cyber extortion coverage reimburses individuals for payments they made under the duress of an extortion threat.
- *Online fraud* ( $L_5$ ). Online frauds include the direct financial losses caused by cyber attacks, such as stolen account funds, unauthorized use of banking or credit cards, phishing schemes, and other types of fraud. Online fraud coverage pays for the direct financial loss incurred by these attacks.
- *Theft* ( $L_6$ ). Theft refers to the loss incurred by cyber attacks against security systems. For instance, an attacker unlocks the smart lock and steals wealth from policyholders. The theft coverage reimburses the cost of repurchasing items and property loss.

Figure 2 shows those risk categories from the perspectives of insurance companies based on the vulnerability graph.

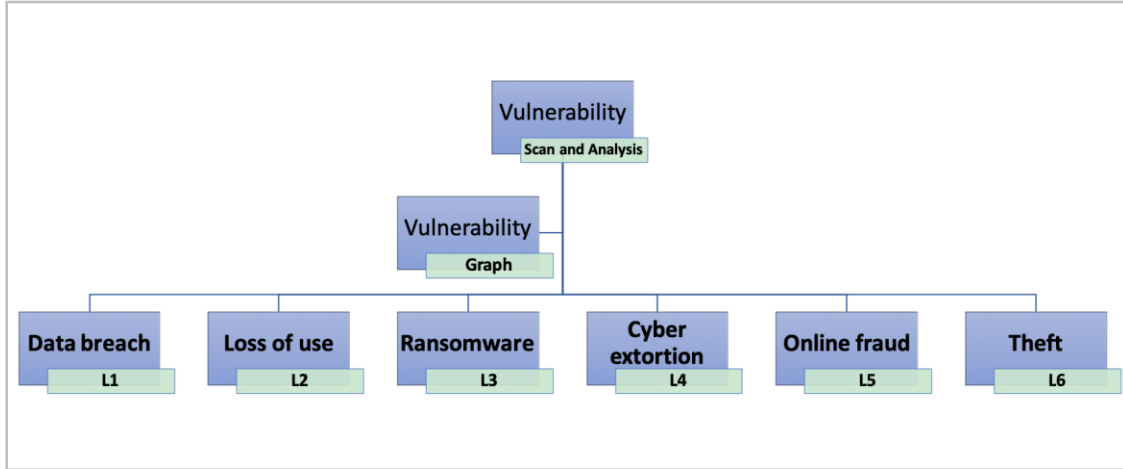
## 2.3 MODELING CYBER RISKS IN THE SMART HOME ECOSYSTEM

It is ideal to patch all the vulnerabilities to mitigate risks. However, it is not always possible in practice (e.g., due to lack of manpower). Thus, assessing the risks of the vulnerability network is essential to optimize



resources and the effort required to protect the network. Analyzing the network risks in isolation offers a limited perspective on network security, given the complex interdependencies between vulnerabilities.

**Figure 2**  
VARIOUS INSURANCE RISKS IN A SMART HOME ECOSYSTEM.



Bayesian Attack Graphs (BAGs) [8, 15] provide a powerful framework to represent prior knowledge about vulnerabilities and network connectivity, depicting the paths of an attacker through the system by exploiting successive vulnerabilities. At a high level, BAGs are graphical models representing information about network vulnerabilities and their interactions, and different paths that an attacker can use to compromise a given objective. Along each attack path, vulnerabilities are exploited in sequence, meaning that each successful exploitation allows the attacker to acquire more privileges toward the target.

**Figure 3**  
ILLUSTRATION OF ATTACK PATHS IN THE SMART HOME ECOSYSTEM.

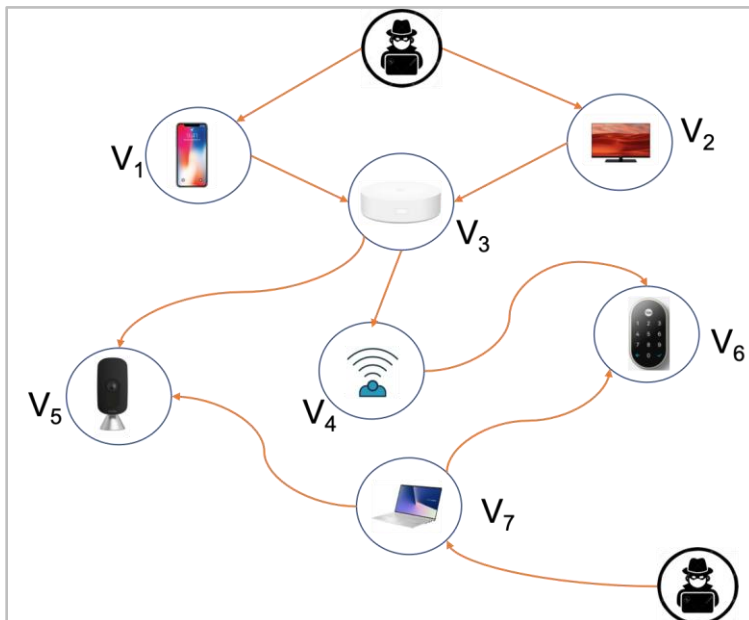


Figure 3 illustrates various attack scenarios, three of which are described in more detail.

- Attack scenario 1: This attack scenario is described in Section 2.1. The attack path is  $V_1 \rightarrow V_3 \rightarrow V_5$ . This attack can cause risks, including data breach (e.g., data stored in the smart hub) and cyber extortion (e.g., private activities captured by the camera).
- Attack scenario 2: The attacker exploits a vulnerability in the smartphone Operating System ( $V_1$ : CVE-2022-22667) over the wireless network, and gains access to the smartphone. The attacker uses this access to compromise the smart home hub in the network by exploiting the vulnerability ( $V_3$ : CVE-2018-3919). Further, a smart sensor vulnerability ( $V_4$ : CVE-2021-39277) can be exploited, and a smart lock vulnerability ( $V_6$ : CVE-2019-12944) can be further exploited to compromise the lock. This attack path can be represented as a path of three edges, namely  $V_1 \rightarrow V_3 \rightarrow V_4 \rightarrow V_6$ . This attack can cause risks, including data breach and property theft (e.g., unlocking the door).
- Attack scenario 3: The attacker exploits a vulnerability in the laptop ( $V_7$ : CVE-2017-8759) over the wireless network, and remotely executes some malicious code. The attacker uses this access to exploit the vulnerability ( $V_5$ : CVE-2021-21736) in the smart camera to gain control over it. This attack can cause risks, including data breach and cyber extortion.

Let  $V_j$  denote the state that vulnerability  $j$  is exploited (i.e., the corresponding smart home device is compromised or not), where  $V_j = 1$  means vulnerability  $j$  is successfully exploited and  $V_j = 0$  the opposite,  $j = 1, 2, \dots, J$ . Let  $L_k$  denote the total loss associated with type  $k$  risk, which is determined by successfully exploiting vulnerabilities,  $k = 1, \dots, M$ . Note that the joint probability of vulnerabilities can be represented via BAG [8]

$$P(V_1 = v_1, \dots, V_N = v_N) = \prod_{i=1}^N P(V_i = v_i | \mathbf{pa}_i), \quad v_i = 1, 0, \quad (1)$$

where  $N$  represents the total number of vulnerabilities,  $\mathbf{pa}_i$  is the parent node sets of vulnerability node  $i$  (e.g., vulnerability node  $V_5$  in Figure 3 has the parent node set  $\mathbf{pa}_5 = \{V_3, V_7\}$ ), and

$$v_i = \begin{cases} 1, & \text{the corresponding device is compromised,} \\ 0, & \text{the corresponding device is not compromised.} \end{cases}$$

Note that for type  $k$  loss, we have

$$\begin{aligned} P(L_k \leq t_k) &= \sum_{\mathbf{V}} P(L_k \leq t | \mathbf{V} = \mathbf{v}) P(\mathbf{V} = \mathbf{v}) \\ &= \sum_{\mathbf{V}} P(L_k \leq t | \mathbf{V} = \mathbf{v}) \prod_{i=1}^N P(V_i = v_i | \mathbf{pa}_i), \end{aligned} \quad (2)$$

where  $k = 1, \dots, M$ , and  $\mathbf{v} = (v_1, \dots, v_N)$ . The distribution of total loss (TL) can be represented by

$$\begin{aligned} P(\text{TL} \leq t) &= P\left(\sum_{k=1}^M L_k \leq t\right) \\ &= \sum_{\mathbf{V}} P(\sum_{k=1}^M L_k \leq t | \mathbf{V} = \mathbf{v}) \prod_{i=1}^N P(V_i = v_i | \mathbf{pa}_i). \end{aligned} \quad (3)$$

From the practical perspective, we study a special case by assuming that any vulnerability that can be exploited will be exploited independently by the attacker. It corresponds to the worst-case scenario, and the joint probability of vulnerabilities can be represented as

$$P(V_1 = v_1, \dots, V_N = v_N) = \prod_{i=1}^N P(V_i = v_i | \mathbf{pa}_i), \quad v_i = 1, 0,$$

This approach is straightforward to implement in practice. However, it overestimates the risk since every vulnerability is assumed to be exploitable and hence, can be considered as a conservative case. For ease of reference, we name this **Approach 1**, and the BAG approach **Approach 2**. Please note that the key difference between Approach 1 and Approach 2 is that Approach 1 does not consider exploitable relationships among vulnerabilities while Approach 2 does.

We also pay special attention to the dependence among large risks, i.e., tail dependence. The relevant concept is recalled as follows: Let  $F_X$  and  $F_Y$  be the distribution of random variable  $X$  and  $Y$ , then the tail dependence [16, 17] index  $\chi(u)$  of  $X$  and  $Y$  at the level  $u$  is

$$\chi(u) = P((Y > F_Y^{-1}(u) | X > F_X^{-1}(u))).$$

The sample version of  $\chi(u)$ , based on data  $\{(x_i, y_i) | i = 1, \dots, n\}$  is

$$\chi_n(u) = \frac{1}{n(1-u)} \sum_{i \leq n} I\{x_i > x_{[nu]:n}, y_i > y_{[nu]:n}\},$$

where  $x_{[nu]:n}$  and  $y_{[nu]:n}$  represent the  $[nu]$ th order statistics, respectively.

In the following section, we discuss two scenarios.

### 2.3.1 SCENARIO WITH FEWER VULNERABILITIES

Assume that a smart home has only three vulnerabilities  $V_1, V_3$  and  $V_5$  as described in attack scenario 1. Table 1 displays the different types of loss caused by successfully exploited vulnerabilities.

**Table 1**  
'x' MEANS VULNERABILITY  $V_i$  CAUSES LOSS  $L_j, i = 1, 3, 5, j = 1, \dots, 5$ ; 'Score' REPRESENTS THE CVSS SCORE; 'Prob.' REPRESENTS THE EPSS PROBABILITY.

CVSS	L <sub>1</sub>	L <sub>2</sub>	L <sub>3</sub>	L <sub>4</sub>	L <sub>5</sub>	L <sub>6</sub>	Score	Prob.
CVE-2022-22667 ( $V_1$ )	x				x		7.8	.02
CVE-2018-3919 ( $V_3$ )	x	x					9.9	.30
CVE-2021-21736 ( $V_5$ )		x		x			7.2	.05

In the following, we discuss different loss distributions.

**Gamma loss distributions** Let  $X_{i,j}$  be the type  $j$  loss caused by  $V_i, i = 1, 3, 5; j = 1, \dots, 5$ . Assume that  $X_{i,j}$  follows a Gamma distribution with scale parameter  $\beta = 1$ , and shape parameter  $\alpha_i$ , and

$$(\alpha_1, \alpha_3, \alpha_5) = (5, 1, 2).$$

This means that the different vulnerabilities result in various losses. For example, the data breach caused by  $V_1$  is severer than that by  $V_3$ . It is further assumed that given the exploration status of vulnerabilities, the different types of losses are independent. We study the loss distribution under the two different approaches in the following.

**Approach 1.** The probabilities of exploitation are independent, i.e.,

$$P(V_1 = v_1, V_3 = v_3, V_5 = v_5) = P(V_1 = v_1)P(V_3 = v_3)P(V_5 = v_5).$$

The probabilities of exploration scenarios can be easily computed in Table 2. For example,

$$P(V_1 = 1, V_3 = 0, V_5 = 0) = .02(1 - .3)(1 - .05) = .0133.$$

Table 2 displays different loss scenarios, where  $X_{i,j} = L_j(\mathbf{s}_i)$  represents the type  $j$  loss caused by scenario  $\mathbf{s}_i, i = 1, \dots, 8$ . Note that for scenarios  $\mathbf{s}_i, i = 1, \dots, 8$ , the loss is computed based on all the vulnerabilities in this scenario, i.e.

$$\begin{aligned} X_{5,j} &\stackrel{d}{=} L_j(\mathbf{s}_2) + L_j(\mathbf{s}_3), & X_{6,j} &\stackrel{d}{=} L_j(\mathbf{s}_3) + L_j(\mathbf{s}_4), \\ X_{7,j} &\stackrel{d}{=} L_j(\mathbf{s}_2) + L_j(\mathbf{s}_4), & X_{8,j} &\stackrel{d}{=} L_j(\mathbf{s}_2) + L_j(\mathbf{s}_3) + L_j(\mathbf{s}_4), \end{aligned}$$

where ' $\stackrel{d}{=}$ ' represents both sides are equal in distribution. For example, we have

$$\begin{aligned} X_{5,1} &\stackrel{d}{=} X_{2,1} + X_{3,1} \\ X_{5,2} &\stackrel{d}{=} X_{3,2}, & X_{5,5} &\stackrel{d}{=} X_{2,5}. \end{aligned}$$

Since  $X_{i,j}$ 's are independent Gamma random variables,  $i = 1, \dots, 4$ , and  $j = 1, \dots, 5$ ,  $X_{k,j}$ 's also Gamma distributions,  $k = 5, \dots, 8$ . The distributions of losses (DLs) are shown in Table 2.

**Table 2**

**VARIOUS LOSS SCENARIOS UNDER DIFFERENT SCENARIOS OF  $(V_1, V_3, V_5)$ . 'Prob.' REPRESENTS THE SCENARIO PROBABILITY, AND 'DL' PRESENTS THE DISTRIBUTION OF LOSS.**

Scenario	$(V_1, V_3, V_5)$	Prob.	$L_1$	$L_2$	$L_4$	$L_5$	$DL_1$	$DL_2$	$DL_4$	$DL_5$
1	(0,0,0)	.6517	0	0	0	0	0	0	0	0
2	(1,0,0)	.0133	$X_{2,1}$	0	0	$X_{2,5}$	$\Gamma(5,1)$	0	0	$\Gamma(5,1)$
3	(0,1,0)	.2793	$X_{3,1}$	$X_{3,2}$	0	0	$\Gamma(1,1)$	$\Gamma(1,1)$	0	0
4	(0,0,1)	.0343	0	$X_{4,2}$	$X_{4,4}$	0	0	$\Gamma(2,1)$	$\Gamma(2,1)$	0
5	(1,1,0)	.0057	$X_{5,1}$	$X_{5,2}$	0	$X_{5,5}$	$\Gamma(6,1)$	$\Gamma(1,1)$	0	$\Gamma(5,1)$
6	(0,1,1)	.0147	$X_{6,1}$	$X_{6,2}$	$X_{6,4}$	0	$\Gamma(1,1)$	$\Gamma(3,1)$	$\Gamma(2,1)$	0
7	(1,0,1)	.0007	$X_{7,1}$	$X_{7,2}$	$X_{7,4}$	$X_{7,5}$	$\Gamma(5,1)$	$\Gamma(2,1)$	$\Gamma(2,1)$	$\Gamma(5,1)$
8	(1,1,1)	.0003	$X_{8,1}$	$X_{8,2}$	$X_{8,4}$	$X_{8,5}$	$\Gamma(6,1)$	$\Gamma(3,1)$	$\Gamma(2,1)$	$\Gamma(5,1)$

Next, we compute the distribution for each business line. Since we assume that the scenarios are independent, it holds that

$$P(L_j \leq t_j) = \sum_{\mathbf{v}} P(L_j \leq t_j | \mathbf{V} = \mathbf{v}) P(\mathbf{v}). \quad (4)$$

For instance, we have

$$\begin{aligned}
P(L_1 \leq t_1) &= .6517 + .0133 \cdot F_5(t_1) + .2793 \cdot F_1(t_1) + .0343 + .0057 \cdot F_6(t_1) + .0147 \\
&\quad \cdot F_1(t_1) + .0007F_5(t_1) + .0003F_6(t_1) \\
&= .686 + .014 \cdot F_5(t_1) + .294 \cdot F_1(t_1) + .006 \cdot F_6(t_1),
\end{aligned}$$

where  $F_\alpha(\cdot) \sim \Gamma(\alpha, 1)$  represents a Gamma distribution with shape parameter  $\alpha$  and scale parameter 1. Similarly, it holds that

$$\begin{aligned}
P(L_2 \leq t_2) &= .665 + .285F_1(t_2) + .035F_2(t_2) + .015F_3(t_2), \\
P(L_4 \leq t_4) &= .95 + .05F_2(t_4), \\
P(L_5 \leq t_5) &= .98 + .02F_5(t_5).
\end{aligned}$$

For the total loss  $TL = L_1 + L_2 + L_4 + L_5$ , we have

$$\begin{aligned}
&P(L_1 + L_2 + L_4 + L_5 \leq t) \\
&= \sum_{\mathbf{v}} P(L_1 + L_2 + L_4 + L_5 \leq t | \mathbf{V} = \mathbf{v}) \prod_{\mathbf{v}} P(\mathbf{v}) \\
&= .6517 + .0133 \cdot F_{10}(t) + .2793 \cdot F_2(t) + .0343 \cdot F_4(t) \\
&\quad + .0057 \cdot F_{12}(t) + .0147 \cdot F_6(t) + .0007F_{14}(t) + .0003F_{16}(t). \tag{5}
\end{aligned}$$

It should be noted that although we assume that given the attack exploration scenario,  $(L_i | \mathbf{v})$ 's are independent,  $L_i$ 's are not independent because of the same vulnerabilities. It is further confirmed in the following discussion.

- **Simulation.** We perform a simulation study to validate the loss distributions. The simulation algorithm is presented in Algorithm 1. In our case, we have vulnerabilities  $(V_1, V_3, V_5)$ , and the exploration probabilities

$$(e_1, e_3, e_5) = (p_1, p_3, p_5) = (.02, .3, .05).$$

The number of simulations is  $R = 100,000$ .

**Algorithm 1:** Loss simulation in a smart home ecosystem.

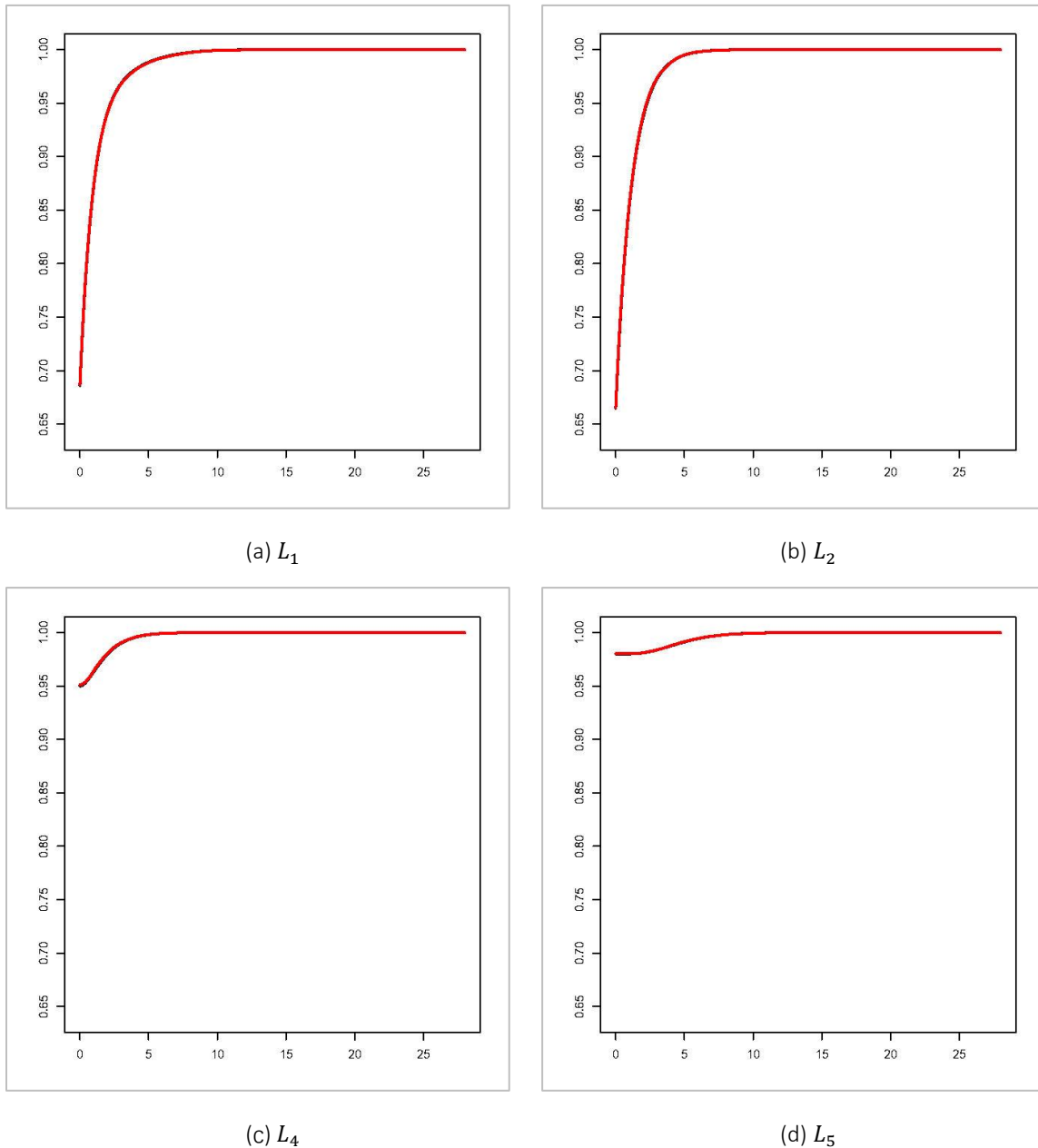
<b>INPUT:</b> Vulnerabilities $(V_1, \dots, V_N)$ ; EPSS probabilities $(p_1, \dots, p_N)$ ; Loss distributions of $X_{i,j}$ 's; Number of simulations $R$ .	
<b>OUTPUT:</b> Loss distributions.	
1	Draw the BAG based on vulnerabilities $(V_1, \dots, V_N)$ ;
2	Determine the exploitation probabilities $(e_1, \dots, e_N)$ based on EPSS probabilities $(p_1, \dots, p_N)$ and the BAG;
3	<b>for</b> $k = 1$ <b>to</b> $R$ <b>do</b>
4	Generate Bernoulli vector $(v_1, \dots, v_N)$ based on $(e_1, \dots, e_N)$ ;
5	Determine business lines that are impacted by each vulnerability $V_i$ with $v_i = 1$ ;
6	Randomly generate losses $x_{i,j}$ 's from their corresponding distributions for those impacted business lines;
7	<b>end</b>
8	Record losses for each business $L_j, j = 1, \dots, M$ .

Figures 4(a), 4(b), 4(c), and 4(d) show the distributions of losses based on Eq.(4) (black color) and the simulation (red color) for  $L_1, L_2, L_4$ , and  $L_5$ , respectively. We observe that the simulated results coincide with theoretical results very well.

Figure 5(a) displays the theoretical distribution of the total loss based on Eq.(5) (black color) and the simulated distribution of the total loss (red color). Again, we observe that they match very well. Figure 5(b) shows all the losses together for comparison. It is seen that  $L_4$  and  $L_5$  are more likely to have small values since they are impacted by  $V_5$  and  $V_1$ , respectively, which have low exploit probabilities. Because  $V_1$  is more difficult to exploit,  $L_5$  is more likely to have a small value than  $L_4$ .  $L_1$  and  $L_2$  are more likely to be large values because of the high exploit probability of  $V_3$ . Table 3 displays the summary statistics of different types of losses and the total loss based on simulation. It is seen that the 95th percentiles of  $L_4$  and  $L_5$  are both 0s which fits the previous conclusion.

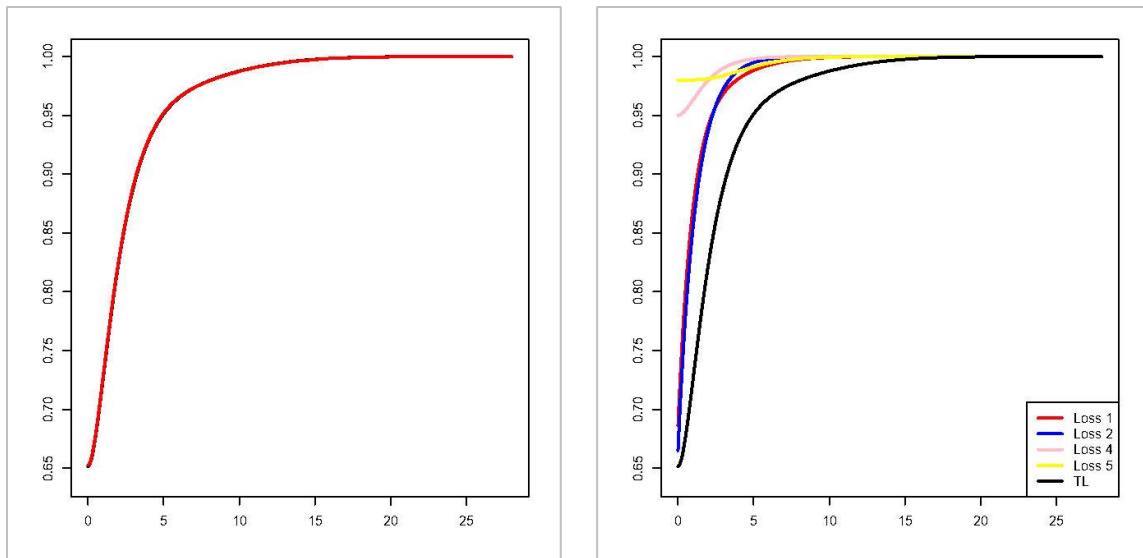
**Figure 4**

**SIMULATED DISTRIBUTIONS (COLORED) AND THEORETICAL DISTRIBUTIONS (BLACK).**



- Dependence among losses.** It is interesting to study the dependence among risks of different business lines. Although it is assumed that the exploitations are independent, the dependence can be caused by the same vulnerability. Table 4 displays Kendall’s tau correlation coefficients between the losses of different business lines based on simulation. It is seen that  $L_1$  and  $L_2$  have a large correlation .691. This can be explained by vulnerability  $V_3$  that affects both business lines and has a large exploit probability .3.  $L_4$  and  $L_5$  are caused by different vulnerabilities; therefore, the correlation is 0. The other small correlations in the table can be explained similarly. In terms of the correlation between each business line and total loss, it is observed that  $L_1$  and  $L_2$  have large correlations. This can be explained by the fact that both business lines have large risks.

**Figure 5**  
 THE SIMULATED DISTRIBUTION (COLORED) OF TOTAL LOSS AND THE THEORETICAL DISTRIBUTION (BLACK) OF TOTAL LOSS.



(a) Distributions of total loss

(b) Simulated distributions of all losses

**Table 3**  
 SUMMARY STATISTICS OF DIFFERENT TYPES OF LOSSES AND THE TOTAL LOSS BASED ON SIMULATION, WHERE ‘SD’ REPRESENTS STANDARD DEVIATION.

	Min	Q <sub>25</sub>	Median	Q <sub>75</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99</sub>	Q <sub>99.5</sub>	Q <sub>99.9</sub>	Max	Mean	SD
$L_1$	.000	.000	.000	.241	1.293	2.261	5.429	6.936	9.650	16.624	.401	1.061
$L_2$	.000	.000	.000	.338	1.429	2.245	4.234	5.000	7.042	13.168	.397	.892
$L_4$	.000	.000	.000	.000	.000	.000	2.926	3.855	5.792	11.753	.097	.529
$L_5$	.000	.000	.000	.000	.000	.000	4.592	6.213	9.304	15.595	.099	.768
TL	.000	.000	.000	1.208	3.205	4.900	1.844	13.191	17.473	27.579	.995	2.142

Table 4 also shows the tail indexes  $\chi_u$ s with  $u = .999$  between different losses. It is interesting to see that  $L_1$  and  $L_5$  have the largest tail dependence .060 although  $L_1$  and  $L_2$  have the largest Kendall’s tau correlation. This can be explained by the fact that  $V_1$  affects both  $L_1$  and  $L_5$ , which

can result in large losses. This can also be seen in Table 3 that both  $L_1$  and  $L_5$  have large values of high quantiles (namely,  $Q_{99,9}$ ).

We draw the following insight based on the previous discussion:

**Insight 1.** *It is practical to assume that any vulnerability that can be exploited will be exploited independently by the attacker in a smart home system. However, there exists dependence among different business risks if a common vulnerability exists, and the tail dependence between business lines can also exist.*

**Table 4**

KENDALL'S TAU CORRELATION COEFFICIENTS AND TAIL INDEXES  $\chi(.999)$ S BETWEEN DIFFERENT LOSSES.

	Kendall's tau				Tail index $\chi(.999)$			
	$L_2$	$L_4$	$L_5$	TL	$L_2$	$L_4$	$L_5$	TL
$L_1$	.691	-.007	.266	.817	.000	.000	.060	.420
$L_2$		.352	.002	.861		.030	.000	.040
$L_4$			.000	.352			.000	.020
$L_5$				.258				.380

**Approach 2** In this case, the exploitations of vulnerabilities are not independent. Based on the BAG:  $V_1 \rightarrow V_3 \rightarrow V_5$ , the joint distribution of  $(V_1, V_3, V_5)$  can be represented as

$$P(V_1, V_3, V_5) = P(V_1)P(V_3|V_1)P(V_5|V_3).$$

For comparison, we assume that  $P(V_1 = 1) = .02$ ,  $P(V_3 = 1|V_1 = 1) = .3$ , and  $P(V_5 = 1|V_3 = 1) = .05$ . The possible scenarios are less compared to Table 2, i.e., 1, 2, 5, and 8. Table 5 shows the probabilities of different scenarios, and also the loss distributions.

**Table 5**

VARIOUS LOSS SCENARIOS UNDER DIFFERENT SCENARIOS OF  $(V_1, V_3, V_5)$ . 'Prob.' REPRESENTS THE SCENARIO PROBABILITY, AND 'DL' PRESENTS THE DISTRIBUTION OF LOSS.

Scenario	$(V_1, V_3, V_5)$	Prob.	$L_1$	$L_2$	$L_4$	$L_5$	$DL_1$	$DL_2$	$DL_4$	$DL_5$
1	(0,0,0)	.980	0	0	0	0	0	0	0	0
2	(1,0,0)	.014	$X_{2,1}$	0	0	$X_{2,5}$	$\Gamma(5,1)$	0	0	$\Gamma(5,1)$
5	(1,1,0)	.0057	$X_{5,1}$	$X_{5,2}$	0	$X_{5,5}$	$\Gamma(6,1)$	$\Gamma(1,1)$	0	$\Gamma(5,1)$
8	(1,1,1)	.0003	$X_{8,1}$	$X_{8,2}$	$X_{8,4}$	$X_{8,5}$	$\Gamma(6,1)$	$\Gamma(3,1)$	$\Gamma(2,1)$	$\Gamma(5,1)$

We compute the distribution for each business line based on Eq.(2). For example, we have

$$\begin{aligned} & P(L_1 \leq t_1) \\ &= \sum_{\mathbf{v}} P(L_1 \leq t_1 | V_1 = v_1, V_3 = v_3, V_5 = v_5) P(V_1 = v_1) P(V_3 = v_3 | V_1 = v_1) P(V_5 = v_5 | V_3 = v_3) \\ &= .98 + .014 \cdot F_5(t_1) + .006 \cdot F_6(t_1), \end{aligned}$$

Similarly, it holds that

$$P(L_2 \leq t_2) = .994 + .0057F_1(t_2) + .0003F_3(t_2),$$



$$P(L_4 \leq t_4) = .9997 + .0003F_2(t_4),$$

$$P(L_5 \leq t_5) = .98 + .02F_5(t_5).$$

The distribution of total loss can be presented as

$$P(L_1 + L_2 + L_4 + L_5 \leq t)$$

$$= \sum_{\mathbf{V}} P(L_1 + L_2 + L_4 + L_5 \leq t | \mathbf{V} = \mathbf{v}) P(V_1 = v_1) P(V_3 = v_3 | V_1 = v_1) P(V_5 = v_5 | V_3 = v_3)$$

$$= .98 + .014 \cdot F_{10}(t) + .0057 \cdot F_{12}(t) + .0003F_{16}(t). \quad (6)$$

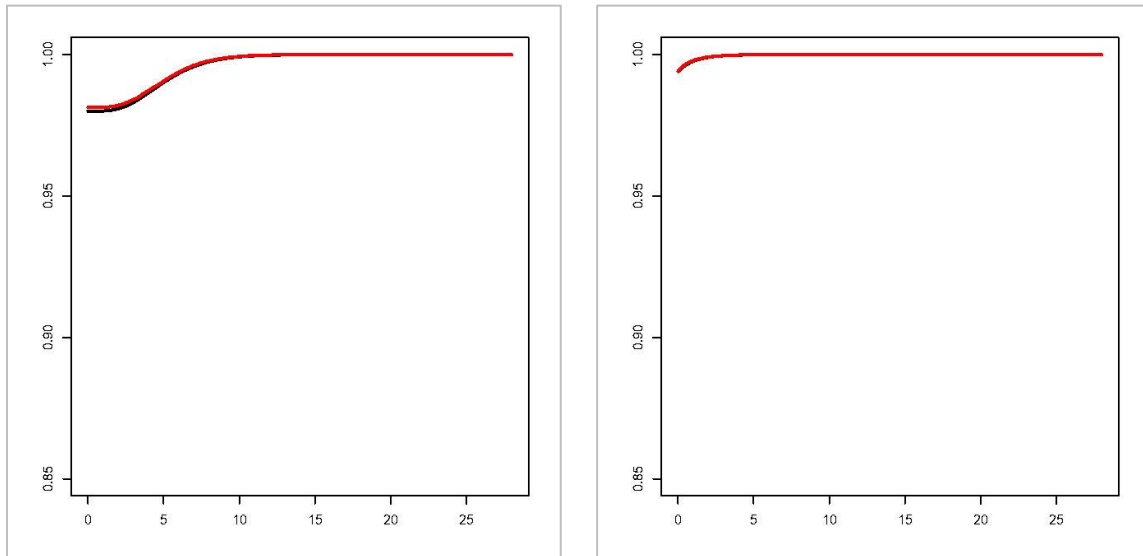
- **Simulation.** We also perform a simulation study to verify the loss distributions using Algorithm 1. In our case, the exploitation probabilities are

$$(e_1, e_3, e_5) = (.02, .3, .05).$$

The number of simulations is also set to be  $R = 10,000$ .

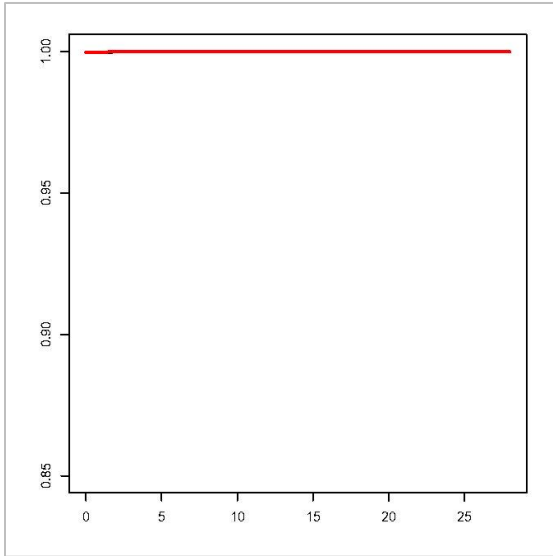
Figure 6

SIMULATED DISTRIBUTIONS (COLORED) AND THEORETICAL DISTRIBUTIONS (BLACK).

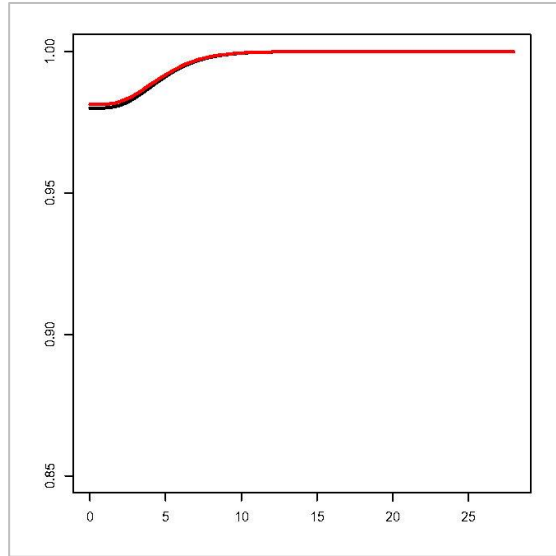


(a)  $L_1$

(b)  $L_2$



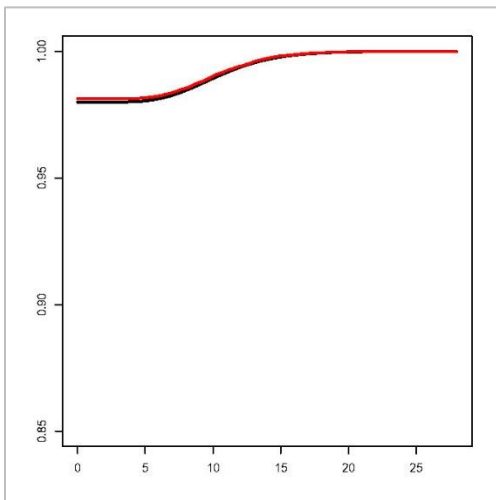
(c)  $L_4$



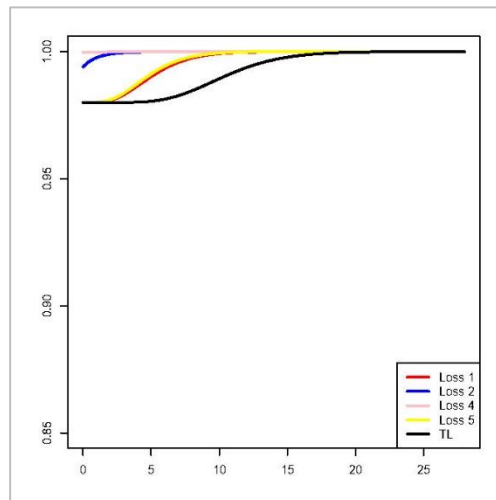
(d)  $L_5$

The distributions of different losses based on the BAG approach are displayed in Figure 6. It can be observed that the simulated distributions (black) coincide with the theoretical results (red). Figure 7(a) displays the theoretical distribution of the total loss based on Eq.(6) (black color) and the simulated distribution of the total loss (red color). We again observe that they match very well. Figure 7(b) shows all the losses together for comparison.  $L_4$  is more likely to have smaller values than  $L_2$ . This can be explained by the fact that  $V_5$ , which leads to  $L_4$ , is the most difficult vulnerability to exploit since it can only be exploited after both  $V_1$  and  $V_3$  are successfully exploited. Since  $V_3$  is relatively easier to exploit than  $V_5$ ,  $L_2$  affected by  $V_3$  and  $V_5$ , it is more likely to have larger values compared to  $L_4$ . Compared with  $L_4$  and  $L_2$ ,  $L_1$  and  $L_5$  are less likely to have small values since  $V_1$  and  $V_3$  are exploited first.

**Figure 7**  
**THE SIMULATED DISTRIBUTION (COLORED) OF TOTAL LOSS AND THE THEORETICAL DISTRIBUTION (BLACK) OF TOTAL LOSS.**



(a) Distributions of total loss



(b) Simulated distributions of all losses

Table 6 displays the summary statistics of different types of losses and the total loss. Compared to Table 3, it is seen that  $L_1$  and  $L_2$ , and TL are more likely to have small values. The means of losses are less than the corresponding ones by Approach 1. A similar conclusion can also be drawn for the standard deviations. It should also be mentioned that the large losses of TL (namely larger than  $Q_{99}$ ) for both approaches are close. This can be explained by the fact that  $L_1$  and  $L_5$  both have  $V_1$  that has a large impact on the total loss.

- **Dependence among losses.** Table 7 displays Kendall's tau correlation coefficients. It is observed  $L_1$  and  $L_5$  has the largest correlation .991, which is different from that in Table 4. This is mainly because  $V_1$ , which needs to be exploited first affects both  $L_1$  and  $L_5$ . It is interesting to see that  $L_2$  and  $L_5$  have a large correlation .551 although they do not have a shared vulnerability. This strong dependence is caused by the chain relation in the BAG. We also observe that  $L_1$  and  $L_5$  are strongly correlated with TL as they are related to  $V_1$ . Since  $V_5$  is the last to exploit, this results in less dependence of  $L_4$  on TL.

The tail indexes  $\chi_u$ s with  $u = .999$  between different losses are also shown in Table 7. We again observe that  $L_1$  and  $L_5$  have the largest tail dependence, and both have large tail dependence with the total loss.

**Table 6**  
SUMMARY STATISTICS OF DIFFERENT TYPES OF LOSSES AND THE TOTAL LOSS BASED ON SIMULATION,  
WHERE 'SD' REPRESENTS STANDARD DEVIATION.

	Min	$Q_{25}$	Median	$Q_{75}$	$Q_{90}$	$Q_{95}$	$Q_{99}$	$Q_{99.5}$	$Q_{99.9}$	Max	Mean	SD
$L_1$	.000	.000	.000	.000	.000	.000	4.844	6.487	9.314	17.176	.099	.780
$L_2$	.000	.000	.000	.000	.000	.000	.000	.144	1.811	7.652	.006	.113
$L_4$	.000	.000	.000	.000	.000	.000	.000	.000	.000	4.738	.001	.037
$L_5$	.000	.000	.000	.000	.000	.000	4.463	6.098	9.011	18.827	.093	.737
TL	.000	.000	.000	.000	.000	.000	9.912	12.501	16.440	27.260	.198	1.505

**Table 7**  
KENDALL'S TAU CORRELATION COEFFICIENTS AND TAIL INDEXES  $\chi(.999)$ S BETWEEN DIFFERENT LOSSES.

	Kendall's tau				Tail index $\chi(.999)$			
	$L_2$	$L_4$	$L_5$	TL	$L_2$	$L_4$	$L_5$	TL
$L_1$	.552	.123	.991	.996	.040	.010	.060	.420
$L_2$		.223	.551	.554		.019	.000	.017
$L_4$			.123	.124			.020	.012
$L_5$				.995				.350

**Insight 2.** The BAG has a significant impact on the loss distributions and tail dependence. It is recommended to use the BAG approach to assessing the risks. Approach 1 can be useful for the tail risk assessment of total loss if the total loss is mainly affected by some risks with vulnerabilities that can be easily exploited.

**General loss distributions** Now, we study the impacts of different loss distributions. Assume that  $L_1, L_2, L_4, L_5$  have different distributions:

$$L_1 \sim \Gamma(\alpha_1 V_1 + \alpha_3 V_3, \beta), \quad (7)$$

$$L_2 \sim \text{Lognormal}(\mu_3 V_3 + \mu_5 V_5, \sigma^2), \quad (8)$$

$$L_4 \sim \exp(\lambda_5 V_5), L_5 \sim \exp(\lambda_1 V_1). \quad (9)$$

Let  $(\alpha_1, \alpha_3, \beta) = (5, 1, 1)$ ,  $(\mu_3, \mu_5, \sigma) = (1, 2, 1)$ , and  $(\lambda_1, \lambda_5) = (.2, .5)$ . Under this setting,  $L_2$  has a heavy tail distribution that can lead to a significant loss. We perform a simulation study based on Algorithm 1 by using the above loss distributions, and the other settings are kept the same.

Table 8 shows the summary statistics of losses of each business line and TL. It is seen that  $L_2$  has significantly larger values compared to the others for both Approach 1 and Approach 2.

Further, the  $Q_{99}$  of  $L_2$  by Approach 1 is much larger than that by Approach 2 (31.027 vs 0). This is because  $L_2$  having vulnerabilities  $V_3$  and  $V_5$  can only be exploited after  $V_1$  is successfully exploited for Approach 2. Since the exploitation probability for  $V_1$  is small (.02), this leads to the small values in Approach 2. Similarly, we observe that the total loss of Approach 2 is also much smaller.

**Table 8**

**SUMMARY STATISTICS OF SIMULATED LOSSES BASED ON APPROACH 1 AND APPROACH 2.**

	Min	$Q_{25}$	Median	$Q_{75}$	$Q_{90}$	$Q_{95}$	$Q_{99}$	$Q_{99.5}$	$Q_{99.9}$	Max	Mean	SD
<b>Approach 1</b>												
$L_1$	.000	.000	.000	.243	1.310	2.255	5.398	6.884	9.657	17.148	.403	1.056
$L_2$	.000	.000	.000	1.569	5.791	1.526	31.027	45.978	101.570	587.541	2.223	8.319
$L_4$	.000	.000	.000	.000	.000	.046	3.241	4.542	7.780	15.023	.100	.619
$L_5$	.000	.000	.000	.000	.000	.000	3.463	7.119	14.583	41.677	.102	1.001
TL	.000	.000	.000	2.821	7.908	13.200	33.451	48.243	103.804	588.319	2.828	8.848
<b>Approach 2</b>												
$L_1$	.000	.000	.000	.000	.000	.000	4.934	6.731	9.374	18.485	.105	.811
$L_2$	.000	.000	.000	.000	.000	.000	.000	.968	7.696	328.126	.036	1.388
$L_4$	.000	.000	.000	.000	.000	.000	.000	.000	.000	8.852	.000	.042
$L_5$	.000	.000	.000	.000	.000	.000	3.315	6.841	14.932	33.404	.099	.993
TL	.000	.000	.000	.000	.000	.000	1.197	14.825	24.618	334.562	.240	2.319

Table 9 shows Kendall's tau correlation coefficients and tail indexes. We again observe that  $L_1$  and  $L_2$  have the largest Kendall's tau correlation (.685) for Approach 1, and  $L_1$  and  $L_5$  have the largest Kendall's tau correlation (.990) for Approach 2. For the tail dependence, it is seen that  $L_2$  dominates the tail dependence with the total loss for Approach 1, and the others are negligible. This is because the tail loss of  $L_1$  is much larger than the others. However, it is not true for Approach 2 since we also observe that  $L_5$  has a large tail dependence with the total loss. This is because that i)  $V_1$  is the first vulnerability to be exploited which determines  $L_5$ ; ii) Once  $V_1$  is exploited,  $L_5$  with an exponential distribution with a rate .2 that can produce a relatively large value (e.g.,  $Q_{99.9} = 14.932$ ).

**Table 9**  
KENDALL'S TAU CORRELATION COEFFICIENTS AND TAIL INDEXES  $\chi(.999)$ S BETWEEN DIFFERENT LOSSES.

	$L_2$	$L_4$	$L_5$	TL	$L_2$	$L_4$	$L_5$	TL
	<b>Kendall's tau</b>							
	<b>Approach 1</b>				<b>Approach 2</b>			
$L_1$	.685	0	.269	.764	.542	.104	.990	.993
$L_2$		.366	-.001	.919		.193	.540	.545
$L_4$			-.002	.362			.104	.106
$L_5$				.225				.995
	<b>Tail index <math>\chi(.999)</math></b>							
$L_1$	.000	.000	.050	.000	.050	.020	.030	.090
$L_2$		.010	.000	.990		.019	.007	.510
$L_4$			.000	.010			.000	.016
$L_5$				.000				.520

We draw the following insight based on the discussion:

**Insight 3.** A business line with heavy tail distribution dominates the total loss.

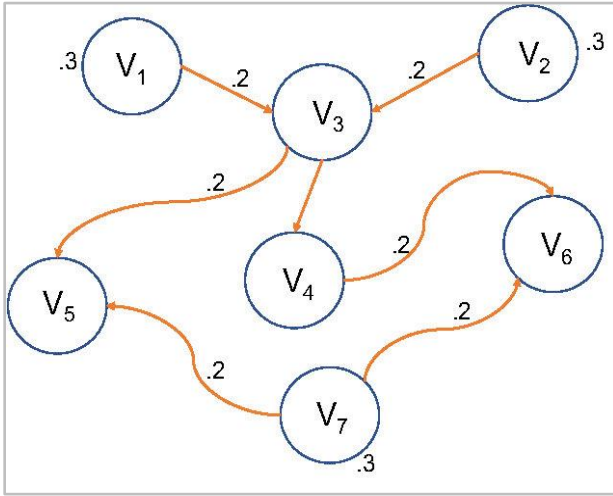
### 2.3.2 SCENARIO WITH MORE VULNERABILITIES

We consider the scenario with more vulnerabilities in Figure 3. Table 10 shows the impacts of each vulnerability. For simplicity, we assume that the outside exploitation probability for  $V_1, V_2, V_7$  is .3, and the inside exploration is .2. The BAG is displayed in Figure 8 according to vulnerabilities.

**Table 10**  
'X' MEANS VULNERABILITY  $V_i$  CAUSES LOSS  $L_j, i = 1, \dots, 7, j = 1, \dots, 6$ ;

CVSS	$L_1$	$L_2$	$L_3$	$L_4$	$L_5$	$L_6$
CVE-2022-22667 ( $V_1$ )	x				x	
CVE-2021-27943 ( $V_2$ )	x					
CVE-2018-3919 ( $V_3$ )	x	x				
CVE-2021-39277 ( $V_4$ )	x					
CVE-2021-21736 ( $V_5$ )		x		x		
CVE-2019-12944 ( $V_6$ )						x
CVE-2017-8759 ( $V_7$ )	x		x			

**Figure 8**  
BAG IN THE SMART HOME ECOSYSTEM.



For the loss distributions, we assume that  $L_1$  and  $L_2$  follow exponential distributions, i.e.,  $L_1 \sim \exp(\lambda_1)$ , and  $L_2 \sim \exp(\lambda_2)$ , where

$$\lambda_1 = \sum_{i \in \mathcal{L}_A} I(V_i), \quad \lambda_2 = \sum_{j \in \mathcal{L}_B} I(V_j)$$

and  $\mathcal{L}_A = \{1,2,3,4,7\}$ , and  $\mathcal{L}_B = \{3,5\}$ .  $L_3$  and  $L_4$  follow a lognormal distribution, i.e.,  $\text{Lognorm}(\mu, \sigma)$ , where  $(\mu, \sigma) = (1,1)$ .  $L_5$  and  $L_6$  follow a Gamma distribution, i.e.,  $\Gamma(\alpha, \beta)$ , where  $(\alpha, \beta) = (1,1)$ .

The joint probabilities of vulnerabilities can be obtained from Figure 8,

$$\begin{aligned} P(\mathbf{V} = \mathbf{v}) &= P(V_1 = v_1)P(V_2 = v_2)P(V_7 = v_7) \\ &\quad \cdot P(V_3 = v_3 | V_2 = v_2, V_1 = v_1)P(V_5 = v_5 | V_3 = v_3, V_7 = v_7) \\ &\quad \cdot P(V_4 = v_4 | V_3 = v_3)P(V_6 = v_6 | V_4 = v_4, V_7 = v_7). \end{aligned}$$

Note that the exploitation probability of  $V_j$  can be represented as

$$e_j = P(V_j = 1 | \mathbf{pa}_j) = \begin{cases} 0, & \forall V_i \in \mathbf{pa}_j, V_i = 0; \\ 1 - \prod_{V_i \in \mathbf{pa}_j, V_i=1} (1 - e_{ij}), & \text{Otherwise} \end{cases}, \quad (10)$$

where  $e_{ij} = P(V_j = 1 | V_i = 1)$ . For example, given  $V_2 = 1$  and  $V_3 = 1$ , we have

$$e_3 = P(V_3 = 1 | V_2 = 1, V_1 = 1) = 1 - (1 - e_{23})(1 - e_{13}),$$

where  $e_{23} = P(V_3 = 1 | V_2 = 1)$ , and  $e_{13} = P(V_3 = 1 | V_1 = 1)$ . Since we have 7 vulnerabilities in the network, the total number of vulnerability scenarios is  $2^7$ , i.e.,  $128^6$ . Certainly, some of the scenarios have 0

<sup>6</sup> R script is available upon request to compute each scenario's probability.

probabilities due to the BAG. For example, Table 11 presents 5 scenarios with probabilities computed based on Eq. (10). It is seen that scenarios 3 and 5 both have probabilities of 0s.

**Table 11**

'Prob. ' REPRESENTS THE JOINT PROBABILITIES OF VULNERABILITIES IN DIFFERENT SCENARIOS.

Scenario	$V_1$	$V_2$	$V_3$	$V_4$	$V_5$	$V_6$	$V_7$	Prob.
1	0	0	0	0	0	0	0	.343
2	0	0	0	0	0	0	1	.094
3	0	0	0	0	0	1	0	.000
4	0	0	0	0	0	1	1	.024
5	0	0	0	0	1	0	0	.000

Algorithm 1 is used to simulate the losses, where the exploit probability  $e_j$  is computed based on Eq. (10),  $j = 1, \dots, 7$ . The number of simulations is set to be  $R = 10,000$ . Table 12 displays the summary statistics of losses based on the simulation. It is seen that  $L_3$  has the largest mean 1.363 and large values of high quantiles. This is because  $L_3$  depends only on  $V_7$  that has a large probability of being exploited from the outside, and further, it follows a lognormal distribution. Although  $L_4$  also follows the same lognormal distribution, it has less probability of being exploited, as shown in the BAG. Therefore,  $L_4$  has a smaller loss than  $L_3$ . Similar conclusions can be drawn for the other business lines.

Table 13 displays Kendall's tau correlations. It is seen that  $L_1$  has small correlations with  $L_4$  and  $L_6$  since they do not have a common vulnerability;  $L_1$  has common vulnerabilities with  $L_3$  ( $V_7$ ) and  $L_5$  ( $V_1$ ), and they have relatively large correlations since both vulnerabilities can be directly exploited from the outside. Although  $L_1$  has a common ( $V_3$ ) with  $L_2$ , it has a relatively small correlation since  $V_3$  cannot be exploited directly.

**Table 12**

SUMMARY STATISTICS OF DIFFERENT TYPES OF LOSSES AND THE TOTAL LOSS BASED ON THE SIMULATION.

	Min	$Q_{25}$	Median	$Q_{75}$	$Q_{90}$	$Q_{95}$	$Q_{99}$	$Q_{99.5}$	$Q_{99.9}$	Max	Mean	SD
$L_1$	.000	.000	.171	.671	1.432	2.041	3.512	4.137	5.627	8.029	.492	.765
$L_2$	.000	.000	.000	.000	.472	1.149	2.678	3.276	4.667	7.430	.158	.522
$L_3$	.000	.000	.000	1.038	4.199	7.284	17.169	23.212	39.256	78.983	1.363	3.839
$L_4$	.000	.000	.000	.000	.000	1.959	8.299	12.209	22.344	52.349	.353	1.893
$L_5$	.000	.000	.000	.180	1.102	1.844	3.350	4.066	5.629	7.693	.302	.715
$L_6$	.000	.000	.000	.000	.000	.235	1.830	2.594	4.527	9.025	.064	.369
TL	.000	.000	1.060	3.383	7.289	11.169	22.742	28.717	47.767	79.752	2.732	4.867

The other correlations can be interpreted similarly. For the tail dependence, it is seen that the tail dependence between different business lines is small.  $L_3$  and  $L_4$  have significant tail dependence with the total loss. This is mainly due to the lognormal loss, which coincides with the observation from Table 12.

**Table 13**  
KENDALL'S TAU CORRELATION COEFFICIENTS AND TAIL INDEXES  $\chi(.99)$ S BETWEEN DIFFERENT LOSSES.

	Kendall's tau					
	$L_2$	$L_3$	$L_4$	$L_5$	$L_6$	TL
$L_1$	.137	.290	.127	.259	.120	.592
$L_2$		.184	.605	.200	.089	.355
$L_3$			.296	.010	.350	.620
$L_4$				.068	.112	.348
$L_5$					.011	.357
$L_6$						.268
	Tail index $\chi(.99)$					
$L_1$	0	0	.040	.010	0	.020
$L_2$		.020	.060	.020	.020	.050
$L_3$			.010	.010	.030	.660
$L_4$				.030	.000	.330
$L_5$					.010	.010
$L_6$						.020

### Section 3: Systemic risk

In this section, we study a particular kind of risk, namely, *systemic risk*, in a smart home ecosystem which occurs when common vulnerabilities exist in many smart home networks. If an attacker successfully exploits the common vulnerabilities, this can cause catastrophic financial loss for the insurer. For instance, in 2017, the WannaCry ransomware attack targeted the computers running the Microsoft Windows Operating System by locking data and demanding ransom payments in the Bitcoin cryptocurrency. It was estimated that more than 200,000 computers were affected with a financial loss of up to billions of dollars [18]. The infamous ScarePackage ransomware attack reached over 900,000 Android cell phone users in just 30 days. If the user wanted to regain control of the device, they had to pay the criminal several hundred dollars in MoneyPak voucher(s).

Assume there are  $S$  smart homes in an insurance portfolio with common vulnerabilities  $V_1, \dots, V_m$ , and those vulnerabilities can cause a systemic risk. We assume that those vulnerabilities can be independently exploited from the outside. In the following section, we discuss two scenarios of systemic risks.

#### 3.1 RANSOMWARE

A ransomware attack is possible in a smart home ecosystem. For example, the hacker can hack the smart lock to demand ransomware to unlock the door, or a smart thermostat can be hacked and display a message to pay a ransom. Since the ransomware attack typically demands the same amount of money for the systemic risk, the distribution of the total loss can be represented as



$$P(SL_3 \leq t) = \sum_{\mathbf{V}} P(L_3 \leq t/s | \mathbf{V}=\mathbf{v}) \prod_{i=1}^m P(V_i = v_i).$$

This scenario becomes a single-line risk in a smart home, which can be analyzed similarly to those in Section 2.3.1. Note that the loss is enlarged  $S$  times compared to the loss in a single smart home in this scenario.

### 3.2 OTHER ATTACKS

We assume that once a common vulnerability is successfully exploited in one smart home, the other smart homes are subject to the same risk, and the same type of losses are independent and identically distributed. Then, the total loss of line  $i$  can be represented as

$$P(L_i^1 + L_i^2 + \dots + L_i^S \leq t_1) = \sum_{\mathbf{V}} P(L_i^1 + L_i^2 + \dots + L_i^S \leq t_1 | \mathbf{V} = \mathbf{v}) \prod_{i=1}^m P(V_i = v_i),$$

where  $L_i^j$  represents the loss of line  $i$  in smart home  $j$ ,  $j = 1, \dots, S$ .

For illustration, we consider the scenario in Section 2.3.1, i.e., assuming that  $V_1, V_3, V_5$  are common vulnerabilities. The loss distributions are the same as those in Section 2.3.1, and  $S = 100$ .

Table 14 displays summary statistics of loss with different types and total loss. Compared to Table 3, it is seen that the values are much larger. For example, the mean of total loss increases from .995 to 10.296, and particularly, the standard deviation increases from 2.142 to 196.216. The high quantile of  $Q_{99.5}$  increases from 13.191 to 1191.65. This indicates that the systemic risk can indeed cause a huge loss.

**Insight 4.** *The systemic risk in a smart home portfolio can be caused by one or more common vulnerabilities. It can result in a considerable loss. We suggest the insurer assess the systemic risk constantly.*

Table 14

SUMMARY STATISTICS OF LOSS WITH DIFFERENT TYPES AND TOTAL LOSS WITH GAMMA DISTRIBUTION BASED ON SIMULATION.

	Min	$Q_{25}$	Median	$Q_{75}$	$Q_{90}$	$Q_{95}$	$Q_{99}$	$Q_{99.5}$	$Q_{99.9}$	Max	Mean	SD
$L_1$	.000	.000	.000	91.419	105.888	113.108	521.267	59.029	629.788	655.514	4.734	88.769
$L_2$	.000	.000	.000	93.722	108.875	123.842	286.630	306.474	322.289	334.733	38.387	62.190
$L_4$	.000	.000	.000	.000	.000	.000	212.159	218.776	231.933	243.592	9.405	42.480
$L_5$	.000	.000	.000	.000	.000	.000	504.582	519.100	539.208	57.106	11.769	75.954
TL	.000	.000	.000	193.645	217.556	404.460	1039.804	1191.650	1405.556	1672.561	10.296	196.216

## Section 4: Pricing cyber risks in a smart home ecosystem

In the current market, only a few companies provide insurance for smart homes, and the majority provide coverage via a personal cyber insurance policy<sup>7</sup>. According to a survey from Security.org<sup>8</sup>, 83 percent of

<sup>7</sup> <https://www.valuepenguin.com/personal-cyber-home-insurance>

<sup>8</sup> <https://www.security.org/insurance/cyber/cost/>

respondents thought annual premiums of \$25,000 coverage would cost under \$150, while 93 percent thought they would cost less than \$20. That explains why most insurers offer cyber insurance at the cost of less than \$100 in the current market, and some charge even as little as \$10 a month for \$25,000 coverage. There are a limited number of companies that provide coverage for high-value homeowners, and the premiums for those higher-value endorsement range from a few hundred dollars to over a thousand per year, depending on the limit and coverage. For example, a major insurance company provides customized coverage with a limit of up to \$250,000 with a premium of \$1,652 per year. Since the smart home insurance market continues to expand, proper limits and affordable premiums need to be further studied. To address this, in the following, we discuss the pricing strategies for cyber risks in a smart home ecosystem.

Based on the loss analysis in the previous sections, we consider the following actuarial premium principles:

- Expectation principle:  $\rho_1(L) = (1 + \theta)E[L]$ , where  $\theta > 0$  is the loading parameter that reflects the risk preferences of the insurer.
- Standard deviation principle:  $\rho_2(L) = E[L] + \theta\sqrt{\text{Var}(L)}$ .
- Gini mean difference (GMD) principle:  $\rho_3(L) = E[L] + \theta\text{GMD}(L)$  where

$$\text{GMD}(L) = E[|L_1 - L_2|],$$

is a statistical measure of variability, and  $L_1$  and  $L_2$  be a pair of independent copies of  $L$ ; see [19, 20].

- Conditional tail expectation:

$$\rho_4(L) = E[L|L \geq \text{VaR}_\beta],$$

where  $\text{VaR}_\beta$  is the value-at-risk at level  $\beta \in (0,1)$

$$\text{VaR}_\beta = \min_{\gamma} \{\gamma : P(L \leq \gamma) \geq \beta\},$$

For more details on the conditional tail expectation, please refer to [21, 22].

In the following, we consider the attack scenario in Figure 3. Similar to Section 2.3.2, we use the BAG approach. To mimic the risk in practice, we assume that the outside exploitation probability for  $V_1, V_2$ , and  $V_7$  are .01, .02, and .9, respectively. Further, the inside exploration probability is .01. For the loss distributions, we assume that  $L_1$  and  $L_2$  follow exponential distributions, i.e.,  $L_1 \sim \exp(\lambda_1)$ , and  $L_2 \sim \exp(\lambda_2)$ , where

$$\lambda_1 = \sum_{i \in \mathcal{L}_A} \alpha_1 I(V_i), \quad \lambda_2 = \sum_{j \in \mathcal{L}_B} \alpha_2 I(V_j)$$

and  $\mathcal{L}_A = \{1,2,3,4,7\}$ ,  $\mathcal{L}_B = \{3,5\}$ , and

$$\alpha_1 = (1/160, 1/32, 1/80, 0, 0, 1/160), \quad \alpha_2 = (0, 0, 1/640, 0, 1/320, 0, 0).$$

$L_3$  and  $L_4$  follow a lognormal distribution,  $\text{Lognorm}(\mu, \sigma)$ , where  $(\mu, \sigma) = (7, 1)$ .  $L_5$  and  $L_6$  follow Gamma distributions, i.e.,  $L_5 \sim \Gamma(\alpha_1, \beta)$ , and  $L_6 \sim \Gamma(\alpha_2, \beta)$ , where  $(\alpha_1, \alpha_2, \beta) = (1000, 2000, 1)$ .

Algorithm 1 is again used to simulate the losses, and the exploit probability  $e_j$  is also computed based on Eq. (9),  $j = 1, \dots, 7$ . The number of simulations is set to be  $R=10,000$ . Table 15 displays the summary statistics of losses based on the simulation. We observe huge losses under some scenarios (e.g., high quantiles of  $L_4$  and  $L_6$ ).

**Table 15**  
SUMMARY STATISTICS OF DIFFERENT TYPES OF LOSSES AND THE TOTAL LOSS BASED ON THE SIMULATION.

	Min	Q <sub>25</sub>	Median	Q <sub>75</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99</sub>	Q <sub>99.5</sub>	Q <sub>99.9</sub>	Max	Mean	SD
L <sub>1</sub>	.00	28.31	92.35	204.10	354.61	476.86	749.93	867.01	1143.49	1875.83	144.81	165.50
L <sub>2</sub>	.00	.00	.00	.00	.00	.00	.00	199.73	704.06	1388.21	3.02	43.15
L <sub>3</sub>	.00	21.26	48.13	99.59	191.60	273.29	57.05	727.44	1047.45	4597.62	83.16	123.43
L <sub>4</sub>	.00	.00	.00	.00	.00	.00	.00	868.25	4867.59	15563.73	18.80	319.33
L <sub>5</sub>	.00	.00	.00	.00	.00	.00	.00	998.13	1029.31	1069.61	9.46	96.69
L <sub>6</sub>	.00	.00	.00	.00	.00	.00	.00	2004.76	2072.27	2150.52	19.70	198.09
TL	.00	87.22	181.37	332.07	539.64	771.11	2142.00	2458.68	5326.47	16521.96	278.95	465.62

#### 4.1 PRICING BASED ON THE MARKET DATA

In this section, we study the pricing strategies based on market data. For comparison purposes, we consider the premium charged by a company (A) with \$1,000 deductible and \$50,000 coverage limit for one year policy period. Company A provides coverage for the following risks: cyber extortion, data restoration, crisis management, and cyber bullying. The yearly premiums are displayed in Table 16. Since we have the same business line L<sub>4</sub> (e.g. cyber extortion), it is used as a standard to determine the parameters in our pricing formulas. Specifically, we fix the premium for L<sub>4</sub> as 28, and determine the parameters in  $\rho_1$  to  $\rho_4$  based on the simulated losses. The parameters are .5, .03, .25, and .34, respectively. The deductible and coverage limit remain the same as those of company A.

**Table 16**  
CYBER INSURANCE OFFERED BY COMPANY A WITH \$1,000 DEDUCTIBLE AND \$50,000 COVERAGE LIMIT FOR ONE YEAR POLICY PERIOD.

Coverage type	Cyber extortion	Data restoration	Crisis management	Cyber bullying	Total Premium
Premium	28	151	231	28	438

Table 17 shows the premium for each business line under different premium principles. The total premium is the sum of all premiums. In addition, we compute the premium based on the aggregated loss.

**Table 17**  
PREMIUMS UNDER DIFFERENT PRICING PRINCIPLES, WHERE 'Total premium' IS THE SUM OF ALL PREMIUMS, AND 'Premium\*' REPRESENTS THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.

Premium	$\rho_1$	$\rho_2$	$\rho_3$	$\rho_4$
L <sub>1</sub>	217	150	185	211
L <sub>2</sub>	5	4	5	5
L <sub>3</sub>	125	87	107	120
L <sub>4</sub>	<b>28</b>	<b>28</b>	<b>28</b>	<b>28</b>
L <sub>5</sub>	14	12	14	14
L <sub>6</sub>	30	26	29	30

Total premium	418	307	368	408
Premium*	418	293	355	422

It is seen that for total premium,  $\rho_1$  is the largest (418) while  $\rho_2$  is the smallest (293). For the premium determined from the aggregated loss, we observe similar results. In the following, we assess the performance of premium principles based on the profit and loss ratio (LR):

$$\text{Profit} = \text{Premium} - \text{Claim},$$

$$\text{LR} = \frac{\text{Claim}}{\text{Premium}}$$

We assume that the permissible loss ratio is 40%.

Consider a portfolio with 500 policyholders who purchase smart home insurance policies. The premiums are charged according to Table 17. The loss scenarios of the portfolio are simulated 10,000 times. Table 18 shows the summary statistics of portfolio profit based on the loss of each business line and aggregated loss for different pricing principles. It is observed that, in this case, all the profits are positive.  $\rho_1$  leads to the largest profit, and  $\rho_2$  leads to the minimum profit. All the standard deviations are the same because the coverage limits and deductible are the same. The summary statistics and loss ratios are shown in Table 19. It is seen that the mean loss ratios are very low (namely less than .1) for all premium principles, and the high quantiles of loss ratios (e.g.,  $Q_{99,9}$ ) are still less than 40%. But the worst-case scenarios for  $\rho_2$  and  $\rho_3$  are beyond the permissible loss ratio of 40%.

**Table 18**

**SUMMARY STATISTICS OF PROFITS UNDER DIFFERENT PRICING PRINCIPLES WITH \$1,000 DEDUCTIBLE AND \$50,000 COVERAGE LIMIT, WHERE 'PROFIT' REPRESENTS THE PROFIT BASED ON THE LOSS OF EACH BUSINESS LINE AND 'PROFIT\*' REPRESENTS THE PROFIT BASED ON THE AGGREGATED LOSS.**

		Min	$Q_1$	$Q_5$	$Q_{10}$	$Q_{15}$	$Q_{50}$	$Q_{75}$	Max	Mean	SD
$\rho_1$	Profit	127,549	174,542	183,192	186,869	189,152	196,215	199,612	207,628	195,089	6,429
	Profit*	127,549	174,542	183,192	186,869	189,152	196,215	199,612	207,628	195,089	6,429
$\rho_2$	Profit	72,049	119,042	127,692	131,369	133,652	140,715	144,112	152,128	139,589	6,429
	Profit*	65,049	112,042	120,692	124,369	126,652	133,715	137,112	145,128	132,589	6,429
$\rho_3$	Profit	102,549	149,542	158,192	161,869	164,152	171,215	174,612	182,628	170,089	6,429
	Profit*	96,049	143,042	151,692	155,369	157,652	164,715	168,112	176,128	163,589	6,429
$\rho_4$	Profit	122,549	169,542	178,192	181,869	184,152	191,215	194,612	202,628	190,089	6,429
	Profit*	116,549	163,542	172,192	175,869	178,152	185,215	188,612	196,628	184,089	6,429

**Table 19**  
SUMMARY STATISTICS OF PROFITS UNDER DIFFERENT PRICING PRINCIPLES WITH \$1,000 DEDUCTIBLE AND \$50,000 COVERAGE LIMIT, WHERE 'LR' REPRESENTS THE LR BASED ON THE LOSS OF EACH BUSINESS LINE AND 'LR\*' REPRESENTS THE LR BASED ON THE AGGREGATED LOSS.

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>9.99</sub>	Max	Mean	SD
$\rho_1$	LR	.01	.04	.06	.08	.09	.11	.12	.19	.24	.39	.07	.03
	LR*	.01	.04	.06	.08	.09	.11	.12	.19	.24	.39	.07	.03
$\rho_2$	LR	.01	.06	.08	.11	.12	.14	.17	.26	.32	.53	.09	.04
	LR*	.01	.06	.09	.12	.12	.15	.18	.27	.34	.56	.09	.04
$\rho_3$	LR	.01	.05	.07	.09	.10	.12	.14	.22	.27	.44	.08	.03
	LR*	.01	.05	.07	.10	.10	.12	.15	.22	.28	.46	.08	.04
$\rho_4$	LR	.01	.05	.06	.08	.09	.11	.13	.19	.24	.40	.07	.03
	LR*	.01	.05	.06	.09	.09	.11	.13	.20	.25	.41	.07	.03

It should be pointed out that some companies are charging \$0 deductibles in practice. For example, Company B offers a smart home policy covering cyber extortion and ransomware, cyber financial loss, and cyber personal protection. The coverage and limits are displayed in Table 20. We apply the premium strategy of company B to our simulated portfolio losses. The summary statistics of the profit and loss ratio are shown in Table 21. It can be seen that under this premium strategy, company B can't make a profit, and the mean loss ratio is 1.35, much larger than the permissible loss ratio.

**Table 20**  
SMART HOME INSURANCE POLICY OFFERED BY COMPANY B WITH \$0 DEDUCTIBLE AND \$50,000 COVERAGE LIMIT FOR ALL COVERED EVENTS.

Coverage limit				Premium
Cyber extortion	Cyber financial loss	Cyber personal protection	All covered events	
10,000	50,000	50,000	50,000	200

**Table 21**  
SUMMARY STATISTICS OF PROFIT AND LOSS RATIO UNDER THE PREMIUM STRATEGY OF COMPANY B.

	Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>50</sub>	Q <sub>95</sub>	Q <sub>995</sub>	Q <sub>999</sub>	Max	Mean	SD
Profit	-106,801	-61,674	-51,710	-46,830	-34,010	-20,912	-13,866	-10,635	-4,540	-34,764	9,416
LR	1.05	1.16	1.21	1.24	1.34	1.52	1.65	1.74	2.07	1.35	.09

## 4.2 PRICING STRATEGIES

In this section, we discuss adjusting the premiums under the permissible loss ratio based on the scenario of Table 17.

**Deductible.** We consider different deductibles other than \$1,000 while the premiums and coverage remain the same. In Appendix A, the profits and loss ratios are shown in Tables 24 to 33 under deductibles \$500, \$250, \$200, \$150, and \$100.

We consider two strategies: i) the permissible mean loss ratio is 40%; ii) the permissible high quantile of loss ratios  $Q_{99.5}$  is 40%. Based on Tables 24 to 33, we recommend various deductibles for different pricing principles and show their mean profits in Table 22.

**Table 22**  
**RECOMMENDED DEDUCTIBLES UNDER DIFFERENT PRICING PRINCIPLES. DEDUCTIBLES/MEAN PROFIT 1 AND 2 ARE DETERMINED BASED ON THE MEAN LOSS RATIO AND 99.5TH LOSS RATIO OF 40%, RESPECTIVELY. 'Premium\*' REPRESENTS THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

	Total premium		Coverage limit	Deductible 1	Mean Profit 1	Deductible 2	Mean Profit 2
$\rho_1$	Premium	418	50,000	150	131,809	250	154,670
	Premium*	418	50,000	150	131,809	250	154,670
$\rho_2$	Premium	307	50,000	250	99,170	500	125,380
	Premium*	293	50,000	250	92,170	500	118,380
$\rho_3$	Premium	368	50,000	200	119,583	500	155,880
	Premium*	355	50,000	200	113,083	500	149,380
$\rho_4$	Premium	408	50,000	150	126,809	500	175,880
	Premium*	396	50,000	150	120,809	500	169,880

Compared to Table 18, although the mean profits are reduced, the deductibles can be significantly smaller.

**Premiums.** We fix the coverage limit \$50,000 and the deductible \$1,000 to discuss different premium strategies. Because of the coverage limit and deductible, the premiums based on the four pricing principles are larger than the mean of total loss (i.e., 279). We set different premiums in Table 23, which correspond to 75%, 71%, 70%, 50%, 25%, and 20% of the mean of the total loss, respectively.

It is seen that if the permissible loss ratio of  $Q_{99.5}$  is set to be 40%, the premium is \$198 and the mean profit is \$85,089; if the permissible mean loss ratio is to be 40%, the premium is \$70 and mean profit is \$21,089. Therefore, it is possible for insurers to offer a smart home insurance policy with a low premium (e.g., \$70) but decent coverage (i.e., \$50,000).

**Table 23**  
**SUMMARY STATISTICS OF PROFITS AND LOSS RATIOS WITH \$1,000 DEDUCTIBLE AND \$50,000 COVERAGE**  
**LIMIT.**

Premium		Min	$Q_1$	$Q_5$	$Q_{10}$	$Q_{50}$	$Q_{95}$	$Q_{99.5}$	$Q_{99.9}$	Max	Mean	SD
210	Profit	23,549	70,542	79,192	82,869	92,215	99,089	101,761	102,699	103,628	91,089	6,429
	LR	.01	.04	.06	.07	.12	.25	.38	.47	.78	.13	.06
198	Profit	17,549	64,542	73,192	76,869	86,215	93,089	95,761	96,699	97,628	85,089	6,429
	LR	.01	.04	.06	.07	.13	.26	<b>.40</b>	.50	.82	.14	.06
195	Profit	16,049	63,042	71,692	75,369	84,715	91,589	94,261	95,199	96,128	83,589	6,429
	LR	.01	.04	.06	.07	.13	.26	.41	.50	.84	.14	.07
140	Profit	-11,451	35,542	44,192	47,869	57,215	64,089	66,761	67,699	68,628	56,089	6,429
	LR	.02	.06	.08	.10	.18	.37	.57	.70	1.16	.20	.09
70	Profit	-46,451	542	9,192	12,869	22,215	29,089	31,761	32,699	33,628	21,089	6,429
	LR	.04	.11	.17	.20	.37	.74	1.13	1.41	2.33	<b>.40</b>	.18
56	Profit	-53,451	-6,458	2,192	5,869	15,215	22,089	24,761	25,699	26,628	14,089	6,429
	LR	.05	.14	.21	.25	.46	.92	1.42	1.76	2.91	.50	.23

## Section 5: Conclusion and Discussion

We have presented a practical quantitative framework for insurers to assess and price smart home cyber risks. The framework consists of four components: (i) identifying vulnerability-incurred cyber risks; (ii) classifying cyber risks into business lines; (iii) modeling cyber risks; and (iv) determining insurance premiums and coverages. We discover that common vulnerabilities can cause dependence among different business risks and tail dependence. We recommend the BAG approach for assessing cyber risks in the smart home ecosystem because it can provide more accurate results. It is worth mentioning that a business line with heavy tail distribution dominates the total loss. The systemic risk in a smart home portfolio is caused by one or more common vulnerabilities that can result in a considerable loss. We also recommend different pricing strategies with various deductibles and premiums for smart home policies, which can make the products more attractive in the market.

The current study has some limitations which need to be addressed in future studies. First, the loss distributions and parameters are set based on experience and limited market data. They can be further calibrated when the actual claim data are available. Second, smart homes may have different network structures and protocols, requiring an individualized risk assessment (i.e., individual BAG analysis). This can further enhance the premium strategy by creating individualized smart home policies. However, it requires much effort from insurers, such as security assessment and loss estimation. Third, the coverage of ransomware or extortion may need further attention in practice since the U.S. government strongly discourages all private companies and citizens from paying ransom or extortion demands, and the payment of ransomware claims may lead to some legal issues<sup>9</sup>. Nevertheless, the present study provides practical guidance for insurers to price cyber risks at the initial stage of the development of the smart home insurance market.



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<sup>9</sup> <https://www.fbi.gov/how-we-can-help-you/safety-resources/scams-and-safety/common-scams-and-crimes/ransomware>



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## Appendix A: Various deductibles

**Table 24**

SUMMARY STATISTICS OF PROFITS UNDER \$500 DEDUCTIBLE AND \$50,000 COVERAGE. 'Profit\*' REPRESENTS THE PROFIT BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.

		Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>15</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Max	Mean	SD
$\rho_1$	Profit	112,217	157,355	166,918	170,996	173,536	181,815	186,350	199,217	180,880	7,743
	Profit*	112,217	157,355	166,918	170,996	173,536	181,815	186,350	199,217	180,880	7,743
$\rho_2$	Profit	56,717	101,855	111,418	115,496	118,036	126,315	130,850	143,717	125,380	7,743
	Profit*	49,717	94,855	104,418	108,496	111,036	119,315	123,850	136,717	118,380	7,743
$\rho_3$	Profit	87,217	132,355	141,918	145,996	148,536	156,815	161,350	174,217	155,880	7,743
	Profit*	80,717	125,855	135,418	139,496	142,036	150,315	154,850	167,717	149,380	7,743
$\rho_4$	Profit	107,217	152,355	161,918	165,996	168,536	176,815	181,350	194,217	175,880	7,743
	Profit*	101,217	146,355	155,918	159,996	162,536	170,815	175,350	188,217	169,880	7,743

**Table 25**

SUMMARY STATISTICS OF LOSS RATIOS UNDER \$500 DEDUCTIBLE AND \$50,000 COVERAGE. 'LR\*' REPRESENTS THE LOSS RATIO BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>9.99</sub>	Max	Mean	SD
$\rho_1$	LR	.05	.11	.13	.15	.16	.18	.20	.27	.31	.46	.13	.04
	LR*	.05	.11	.13	.15	.16	.18	.20	.27	.31	.46	.13	.04
$\rho_2$	LR	.06	.15	.18	.21	.22	.25	.27	.37	.43	.63	.18	.05
	LR*	.07	.15	.19	.22	.23	.26	.29	.38	.45	.66	.19	.05
$\rho_3$	LR	.05	.12	.15	.18	.18	.21	.23	.31	.36	.53	.15	.04
	LR*	.06	.13	.15	.18	.19	.21	.24	.32	.37	.55	.16	.04
$\rho_4$	LR	.05	.11	.13	.16	.16	.19	.21	.28	.32	.47	.14	.04
	LR*	.05	.11	.14	.16	.17	.19	.21	.28	.33	.49	.14	.04

**Table 26**

SUMMARY STATISTICS OF PROFITS UNDER \$250 DEDUCTIBLE AND \$50,000 COVERAGE. 'Profit\*' REPRESENTS THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.

		Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>15</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Max	Mean	SD
$\rho_1$	Profit	85,759	129,401	139,186	143,625	146,351	155,495	160,688	178,804	154,670	8,672
	Profit*	85,759	129,401	139,186	143,625	146,351	155,495	160,688	178,804	154,670	8,672
$\rho_2$	Profit	30,259	73,901	83,686	88,125	90,851	99,995	105,188	123,304	99,170	8,672
	Profit*	23,259	66,901	76,686	81,125	83,851	92,995	98,188	116,304	92,170	8,672
$\rho_3$	Profit	60,759	104,401	114,186	118,625	12,1351	130,495	135,688	153,804	129,670	8,672
	Profit*	54,259	97,901	107,686	112,125	114,851	123,995	129,188	147,304	123,170	8,672
$\rho_4$	Profit	80,759	124,401	134,186	138,625	141,351	150,495	155,688	173,804	149,670	8,672
	Profit*	74,759	118,401	128,186	132,625	135,351	144,495	149,688	167,804	143,670	8,672

**Table 27**  
**SUMMARY STATISTICS OF LOSS RATIOS UNDER \$250 DEDUCTIBLE AND \$50,000 COVERAGE. 'LR\*' REPRESENTS THE LOSS RATIO BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>9.99</sub>	Max	Mean	SD
$\rho_1$	LR	.14	.23	.26	.28	.29	.31	.33	.40	.45	.59	.26	.04
	LR*	.14	.23	.26	.28	.29	.31	.33	.40	.45	.59	.26	.04
$\rho_2$	LR	.20	.31	.35	.39	.40	.43	.45	.55	.61	.80	.35	.06
	LR*	.21	.33	.37	.40	.41	.45	.48	.58	.64	.84	.37	.06
$\rho_3$	LR	.16	.26	.29	.32	.33	.36	.38	.46	.51	.67	.30	.05
	LR*	.17	.27	.30	.33	.34	.37	.39	.48	.53	.69	.31	.05
$\rho_4$	LR	.15	.24	.26	.29	.30	.32	.34	.41	.46	.60	.27	.04
	LR*	.15	.24	.27	.30	.31	.33	.35	.43	.47	.62	.27	.04

**Table 28**  
**SUMMARY STATISTICS OF PROFITS UNDER \$200 DEDUCTIBLE AND \$50,000 COVERAGE. 'Profit\*' REPRESENTS THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>15</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Max	Mean	SD
$\rho_1$	Profit	75,128	118,921	128,691	133,275	136,076	145,387	150,741	169,937	144,583	8,870
	Profit*	75,128	118,921	128,691	133,275	136,076	145,387	150,741	169,937	144,583	8,870
$\rho_2$	Profit	19,628	63,421	73,191	77,775	80,576	89,887	95,241	114,437	89,083	8,870
	Profit*	12,628	56,421	66,191	70,775	73,576	82,887	88,241	107,437	82,083	8,870
$\rho_3$	Profit	50,128	93,921	103,691	108,275	111,076	120,387	125,741	144,937	119,583	8,870
	Profit*	43,628	87,421	97,191	101,775	104,576	113,887	119,241	138,437	113,083	8,870
$\rho_4$	Profit	70,128	113,921	123,691	128,275	131,076	140,387	145,741	164,937	139,583	8,870
	Profit*	64,128	107,921	117,691	122,275	125,076	134,387	139,741	158,937	133,583	8,870

**Table 29**  
**SUMMARY STATISTICS OF LOSS RATIOS UNDER \$200 DEDUCTIBLE AND \$50,000 COVERAGE. 'LR\*' REPRESENTS THE LOSS RATIO BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>9.99</sub>	Max	Mean	SD
$\rho_1$	LR	.19	.28	.30	.33	.34	.36	.38	.45	.50	.64	.31	.04
	LR*	.19	.28	.30	.33	.34	.36	.38	.45	.50	.64	.31	.04
$\rho_2$	LR	.25	.38	.41	.45	.46	.49	.52	.62	.68	.87	.42	.06
	LR*	.27	.40	.43	.47	.48	.52	.55	.65	.71	.91	.44	.06
$\rho_3$	LR	.21	.32	.35	.38	.39	.41	.44	.52	.57	.73	.35	.05
	LR*	.22	.33	.36	.39	.40	.43	.45	.53	.59	.75	.36	.05
$\rho_4$	LR	.19	.29	.31	.34	.35	.37	.39	.47	.51	.66	.32	.04
	LR*	.20	.29	.32	.35	.36	.38	.41	.48	.53	.68	.33	.04

**Table 30**  
**SUMMARY STATISTICS OF PROFITS UNDER \$150 DEDUCTIBLE AND \$50,000 COVERAGE. 'Profit\*'**  
**REPRESENTS THE PROFIT BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>15</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Max	Mean	SD
$\rho_1$	Profit	61,749	105,618	115,508	120,208	123,125	132,594	138,089	158,763	131,809	9,059
	Profit*	61,749	105,618	115,508	120,208	123,125	132,594	138,089	158,763	131,809	9,059
$\rho_2$	Profit	6,249	50,118	60,008	64,708	67,625	77,094	82,589	103,263	76,309	9,059
	Profit*	-751	43,118	53,008	57,708	60,625	70,094	75,589	96,263	69,309	9,059
$\rho_3$	Profit	36,749	80,618	90,508	95,208	98,125	107,594	113,089	133,763	106,809	9,059
	Profit*	30,249	74,118	84,008	88,708	91,625	101,094	106,589	127,263	100,309	9,059
$\rho_4$	Profit	56,749	100,618	110,508	115,208	118,125	127,594	133,089	153,763	126,809	9,059
	Profit*	50,749	94,618	104,508	109,208	112,125	121,594	127,089	147,763	120,809	9,059

**Table 31**  
**SUMMARY STATISTICS OF LOSS RATIOS UNDER \$150 DEDUCTIBLE AND \$50,000 COVERAGE. 'LR\*'**  
**REPRESENTS THE LOSS RATIO BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>99.9</sub>	Max	Mean	SD
$\rho_1$	LR	.24	.34	.37	.39	.40	.42	.45	.52	.56	.70	.37	.04
	LR*	.24	.34	.37	.39	.40	.42	.45	.52	.56	.70	.37	.04
$\rho_2$	LR	.33	.46	.50	.54	.55	.58	.61	.70	.76	.96	.50	.06
	LR*	.34	.48	.52	.56	.57	.61	.64	.74	.80	1.01	.53	.06
$\rho_3$	LR	.27	.39	.42	.45	.46	.48	.51	.59	.64	.80	.42	.05
	LR*	.28	.40	.43	.46	.47	.50	.53	.61	.66	.83	.43	.05
$\rho_4$	LR	.25	.35	.37	.40	.41	.44	.46	.53	.58	.72	.38	.04
	LR*	.25	.36	.39	.42	.42	.45	.47	.54	.59	.74	.39	.05

**Table 32**  
**SUMMARY STATISTICS OF PROFITS UNDER \$100 DEDUCTIBLE AND \$50,000 COVERAGE. 'Profit\*'**  
**REPRESENTS THE PROFIT BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>1</sub>	Q <sub>5</sub>	Q <sub>10</sub>	Q <sub>15</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Max	Mean	SD
$\rho_1$	Profit	44,965	89,249	99,248	104,001	107,026	116,589	122,186	144,683	115,821	9,223
	Profit*	44,965	89,249	99,248	104,001	107,026	116,589	122,186	144,683	115,821	9,223
$\rho_2$	Profit	-10,535	33,749	43,748	48,501	51,526	61,089	66,686	89,183	60,321	9,223
	Profit*	-17,535	26,749	36,748	41,501	44,526	54,089	59,686	82,183	53,321	9,223
$\rho_3$	Profit	19,965	64,249	74,248	79,001	82,026	91,589	97,186	119,683	90,821	9,223
	Profit*	13,465	57,749	67,748	72,501	75,526	85,089	90,686	113,183	84,321	9,223
$\rho_4$	Profit	39,965	84,249	94,248	99,001	102,026	111,589	117,186	139,683	110,821	9,223
	Profit*	33,965	78,249	88,248	93,001	96,026	105,589	111,186	133,683	104,821	9,223

**Table 33**  
**SUMMARY STATISTICS OF LOSS RATIOS UNDER \$100 DEDUCTIBLE AND \$50,000 COVERAGE. ‘LR\*’**  
**REPRESENTS THE LOSS RATIO BASED ON THE PREMIUM DETERMINED FROM THE AGGREGATED LOSS.**

		Min	Q <sub>25</sub>	Q <sub>50</sub>	Q <sub>75</sub>	Q <sub>80</sub>	Q <sub>90</sub>	Q <sub>95</sub>	Q <sub>99.5</sub>	Q <sub>9.99</sub>	Max	Mean	SD
$\rho_1$	LR	.31	.42	.44	.47	.48	.50	.53	.59	.63	.78	.45	.04
	LR*	.31	.42	.44	.47	.48	.50	.53	.59	.63	.78	.45	.04
$\rho_2$	LR	.42	.57	.60	.64	.65	.68	.71	.81	.86	1.07	.61	.06
	LR*	.44	.59	.63	.67	.68	.72	.75	.84	.90	1.12	.64	.06
$\rho_3$	LR	.35	.47	.50	.54	.54	.57	.60	.67	.72	.89	.51	.05
	LR*	.36	.49	.52	.56	.56	.59	.62	.70	.75	.92	.52	.05
$\rho_4$	LR	.32	.43	.45	.48	.49	.51	.54	.61	.65	.80	.46	.05
	LR*	.32	.44	.47	.50	.51	.53	.55	.62	.67	.83	.47	.05

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